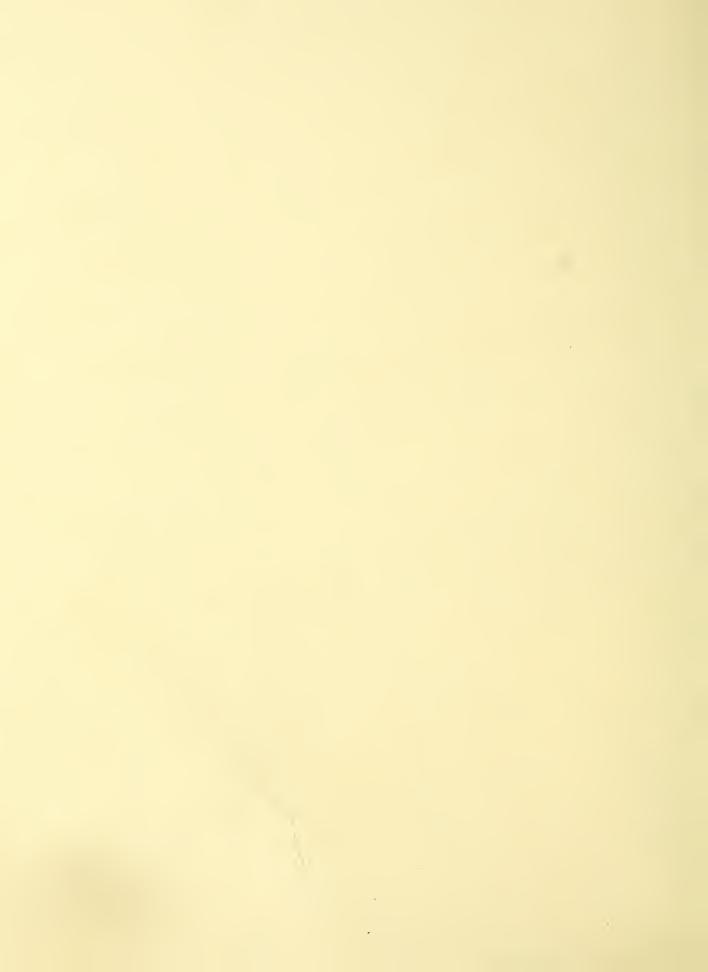
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> U. S. Department of Agriculture Soil Conservation Service Engineering Division

Technical Release No. 42 Design Unit December, 1969

SINGLE CELL RECTANGULAR CONDUITS
CRITERIA AND PROCEDURES FOR STRUCTURAL DESIGN

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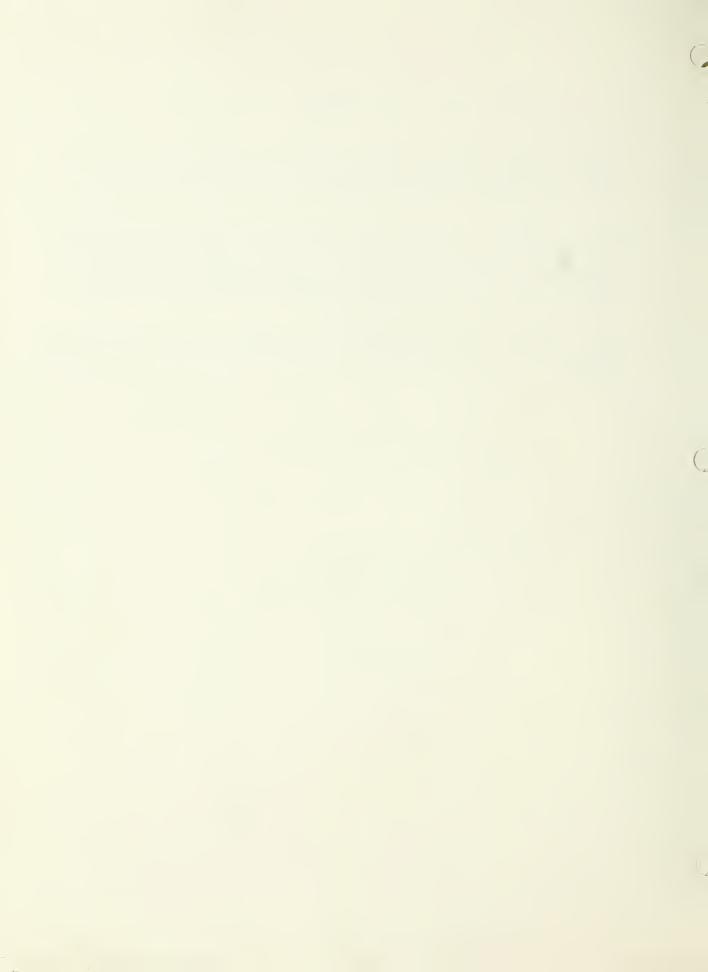


PREFACE

This technical release presents the criteria and procedures established for the structural design of single cell rectangular conduit cross sections. The criteria for these designs has developed over a period of years and has been discussed at various Design Engineers' meetings.

A preliminary set of designs obtained as computer output, was presented and discussed at the Engineering and Watershed Planning Unit-Washington Staff Design Consultation in Columbus, Ohio during July 14-18, 1969. Subsequently, a draft of the subject technical release dated August 14, 1969, was sent to the Engineering and Watershed Planning Unit Design Engineers for their review and comment.

This technical release was prepared by Mr. Edwin S. Alling of the Design Unit, Design Branch at Hyattsville, Maryland. He also wrote the computer program.



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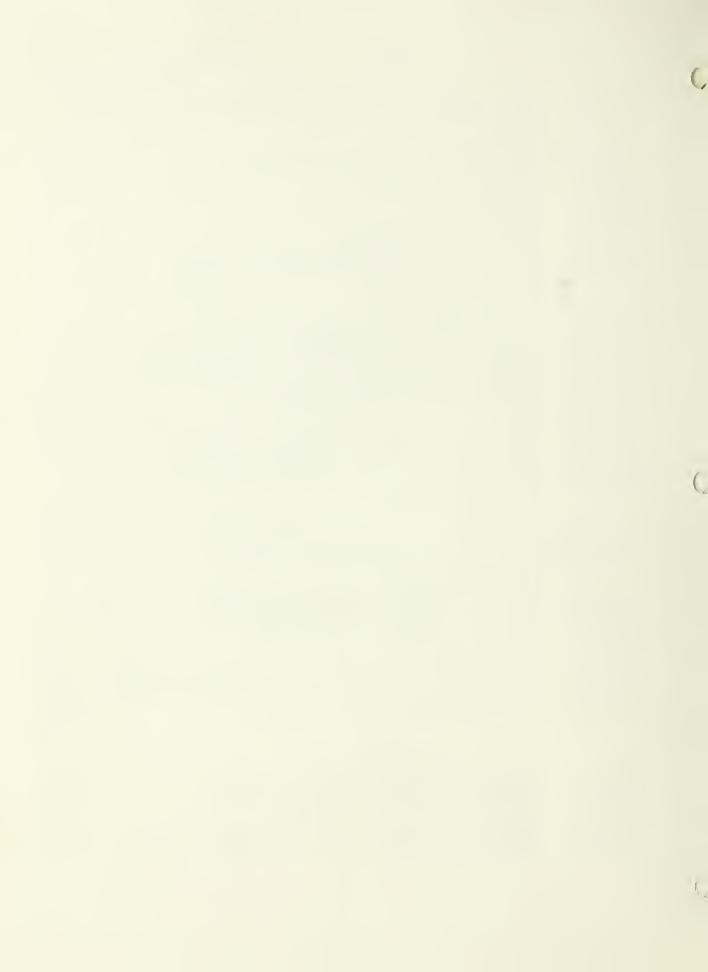
SINGLE CELL RECTANGULAR CONDUITS CRITERIA AND PROCEDURES FOR STRUCTURAL DESIGN

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NOMENCLATURE

Not all nomenclature is listed. Hopefully, the meaning of any unlisted nomenclature may be ascertained from that given.

A = equivalent area of reinforcing steel; total required steel per foot of width

 $A_g \equiv gross area of column$

 $A_s \equiv area of reinforcing steel$

a ≡ ratio used to obtain properties of non-prismatic members

Bl ≡ identification for first basic set of loads, those with the conduit empty

b = width of reinforced concrete member; ratio used to obtain properties of unsymmetrical non-prismatic members

 $b_c \equiv outside width of conduit$

C = carry-over factor; a parameter in the equation for equivalent axial load; a coefficient in the expression for allowable flexural bond stress

 $C_b \equiv carry$ -over factor for bottom slab

 $C_{.TK} \equiv carry$ -over factor from end J to end K

 C_{p} = load coefficient for positive projecting conduits

C_s ≡ carry-over factor for sidewall

 $C_{t} \equiv carry$ -over factor for top slab

D \equiv nominal diameter of reinforcing bar; a parameter in the equation for equivalent axial load

d ≡ effective depth of reinforced concrete member

d'' = d - t/2

 d_{bal} = effective depth for balanced working stresses

 $d_{sh} \equiv \text{effective depth of sidewall at bottom face}$

 d_{st} = effective depth of sidewall at top face or at d_{st} from top face

 $d_{wh} \equiv unit dead weight carried by bottom slab$

 $d_{wt} \equiv unit dead weight of top slab$

 $E \equiv modulus of elasticity$

e = eccentricity of direct force measured from center of section

F = coefficient in the cubic equation used to locate the neutral axis

 $f_c \equiv compressive stress in concrete$

 f_{c} = compressive strength of concrete

 $f_s \equiv stress in reinforcing steel$

 $G \equiv a$ parameter in the equation for equivalent axial load

 H_c = vertical distance from top of conduit to top of embankment

 H_{m} \equiv vertical distance from phreatic surface to top of embankment

 $H_{W} \equiv \text{vertical distance from top of conduit to phreatic surface}$

 $h_c \equiv clear height of conduit$

 $h_{\overline{W}}$ \equiv internal water pressure head measured from the bottom of the

top slab

 $I \equiv moment of inertia$

j = ratio used in reinforced concrete relations

 $K_O \equiv \text{coefficient of lateral pressures at rest}$

k = ratio used in reinforced concrete relations; stiffness coefficient

 $L \equiv \text{span length}$

 $L^{t} \equiv clear span$

IC#1 = load combination number one

 $L_b \equiv bottom slab span$

 $L_D \equiv \text{span between points of inflection}$

 $L_s \equiv sidewall span$

 $L_t \equiv top slab span$

 $M \equiv moment$

 $M_{\Delta} \equiv \text{design moment at } A$

 $M_{ab} \equiv a \text{ moment in ES-28}$

 $M_{\rm B}$ \equiv design moment at top corner diagonal

 $M_{\text{Bi}} \equiv \text{external load corner moment at B for IC}\#\text{i}$

 $M_{Bs} \equiv design$ moment at face of the top support of the sidewall

 M_{Rt} \equiv design moment at face of the support of the top slab

 $M_{\text{Bub}} \equiv \text{corner moment at B for unit load on bottom slab}$

 $M_{Bus} \equiv corner$ moment at B for unit load on sidewalls

 $M_{\text{But}} \equiv \text{corner moment at B for unit load on top slab}$

 $M_{Rhd} \equiv corner$ moment at B for pressure head loading

M_{Rhy} ≡ corner moment at B for hydrostatic sidewall loading

 $M_{JK} \equiv moment at J in span JK$

 M_{Bhy}^{F} = fixed end moment at B for hydrostatic sidewall loading

 $M_{TK}^{F} \equiv \text{fixed end moment at J in span JK}$

 $M_{L^{\dagger}}^{F}$ = fixed end moment for span L[†]

 $M_{\rm S}$ \equiv equivalent moment, moment about axis at the tension steel

 m^{F} = fixed end moment coefficient

 \mathbb{N} \equiv direct force on a section

 $N_b \equiv \text{direct force in bottom slab}$

 $N_{Rk} \equiv \text{direct force on top corner diagonal}$

 $N_C \equiv \text{direct compressive force}$

 $N_S \equiv \text{direct force in sidewall}$

Nt ≡ direct force in top slab; direct tensile force

n ≡ modular ratio; an integer; number of bars per foot of width

 $P \equiv axial column load$

 $p \equiv unit load$

 $p_h \equiv unit load on bottom slab$

p_{bi} ≡ unit load on bottom slab for IC#i

 $p_g \equiv gross steel ratio$

 $p_{h_1} \equiv \text{horizontal unit load corresponding to IC} 1$

 $p_{hd} \equiv unit load for pressure head loading$

 p_{hv} \equiv maximum unit load for hydrostatic sidewall loading

 $p_s \equiv unit load on sidewall$

 $psf \equiv pounds per square foot$

 $p_{si} \equiv unit load on sidewall for IC#i$

 p_t = unit load on top slab; steel ratio for temperature and shrinkage

 $R \equiv reaction$

 $S \equiv stiffness$

 $S_b \equiv stiffness of bottom slab$

 $S_{JK} \equiv stiffness at end J in span JK$

 $S_S \equiv stiffness of sidewall$

 $S_{t} \equiv stiffness of top slab$

 $s \equiv spacing of reinforcing steel$

 $t \equiv thickness$

 $t_b \equiv thickness of bottom slab$

 $t_s \equiv average thickness of sidewall$

 $t_{sb} \equiv thickness of sidewall at the bottom$

 $t_{st} \equiv thickness of sidewall at the top$

 $t_t \equiv thickness of top slab$

u = allowable flexural bond stress in concrete

V ≡ shear

 $V_{b} \equiv \text{shear at bottom face of sidewall}$

 $V_{\mbox{Bt}} \equiv {
m shear} \ {
m at} \ {
m face} \ {
m of} \ {
m support} \ {
m of} \ {
m top} \ {
m slab}$

 $V_{\rm ex}$ \equiv extra shear in sidewall due to loading on top slab

 $V_f \equiv \text{shear at top face of sidewall}$

 V_p \equiv shear at section of maximum positive moment; shear at point of inflection

 V_{t} = shear at top face of sidewall

 $v \equiv allowable shear stress in concrete$

 $W_S \equiv \text{total load on sidewall}$

 $w_{C} \equiv clear \ width \ of \ conduit$

 $x_p \equiv \text{distance from center of top support of sidewall to section of}$

maximum positive moment

 $z \equiv$ eccentricity of direct force measured from the tension steel

 $\gamma_{\rm b}$ \equiv buoyant unit weight of embankment

 $\gamma_{\rm m}$ \equiv moist unit weight of embankment

 $\gamma_{\rm S}$ = saturated unit weight of embankment

 $\gamma_{\rm W}$ = unit weight of water

 θ_{T} = rotation at support J

 ρ = projection ratio for positive projecting conduits

TECHNICAL RELEASE NUMBER 42

SINGLE CELL RECTANGULAR CONDUITS CRITERIA AND PROCEDURES FOR STRUCTURAL DESIGN

Computer Designs

The Soil Conservation Service annually designs a number of cast-in-place rectangular conduits for use in principal and emergency spillways passing through earth embankments. Thorough design of these rectangular conduit cross sections by manual methods is a time consuming process. Because of the statical indeterminacy, the interaction of member thicknesses with moments makes direct design difficult. After an adequate set of member thicknesses is obtained, steel requirements must be completely determined.

A computer program written in FORTRAN for IBM 360 equipment was developed to perform this design task. The program executes the complete structural design of single cell rectangular conduit cross sections given the clear height and width of the conduit, two load combinations, and the design mode. The program was used in the preparation of Technical Release No.43 "Single Cell Rectangular Conduits - Catalog of Standard Designs."

This technical release documents the criteria and procedures used in the computer program. The technical release may be useful as a reference and as a training tool for similar structural problems.

Section Designed

Figure 1 defines the cross sectional shape of the conduit and shows the assumed steel layout. No attempt is made herein to completely identify the computer output listing nor all of the associated nomenclature. This is done in Technical Release No. 43.

The computer program determines the required thicknesses of the top and bottom slabs and the thicknesses at the top and bottom of the sidewalls. Then the computer obtains the minimum acceptable steel areas and maximum acceptable steel spacings at each of the fourteen locations shown in Figure 1. In the case of positive center steel, the spacings actually computed are those required at the respective points of inflection. The computer also determines whether or not any of the positive steel requires definite anchorage at the corners of the conduit.

Loads Specified by User

The design of rectangular conduit sections by the program is independent of the methods by which the user determines his external loads. The user specifies, or selects, unit pressures in two combinations of external loads. These load combinations are defined as:

IC#1 is the load combination having the maximum possible vertical unit load combined with the minimum horizontal unit load consistent with that vertical unit load.

IC#2 is the load combination having the maximum possible horizontal unit load combined with the minimum vertical unit load consistent with that horizontal unit load.

The computer design is adequate for these two load combinations as well as a number of others constructed from them. See page 5 for a more general discussion of loads and load combinations for rectangular conduits.

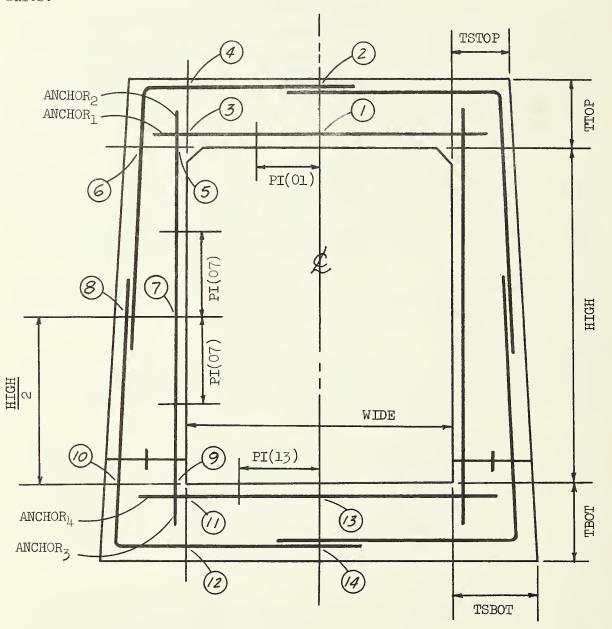


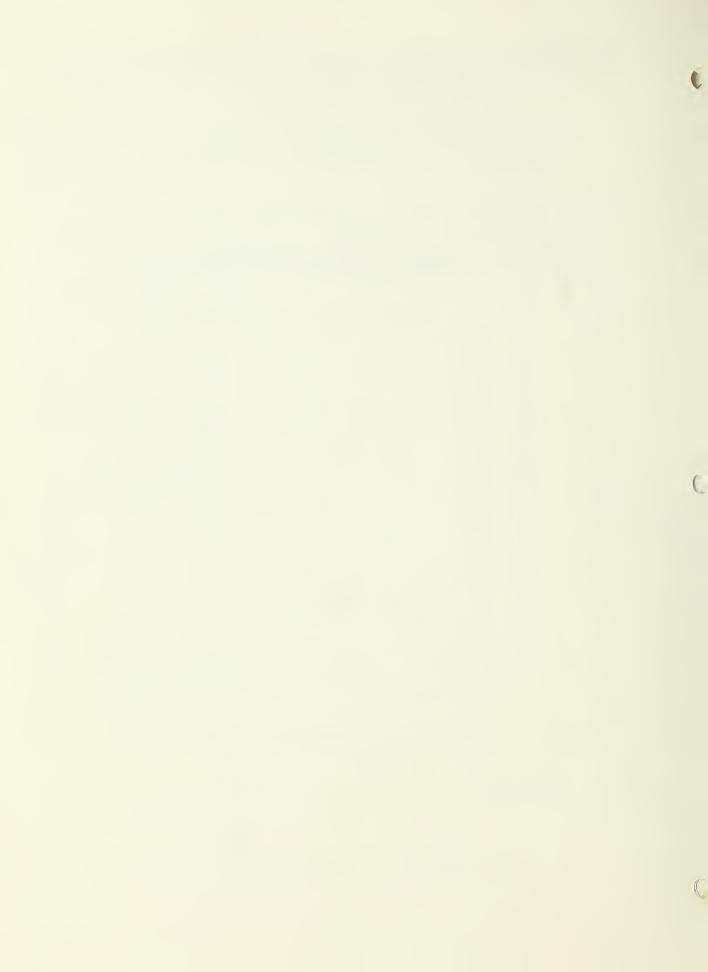
Figure 1. Conduit cross section and steel layout.

Design Mode

The program designs conduit sections in accordance with the design mode. A design mode characterizes the conditions for which the conduit is designed. Four modes are established:

earth foundation, no internal water load $\equiv 00$ earth foundation, with internal water load $\equiv 01$ rock foundation, no internal water load $\equiv 10$ rock foundation, with internal water load $\equiv 11$

The type of foundation assumed in the design governs the number of external load combinations that are considered. Internal water loads are included in the design of pressure conduits. Note that these conduits flow full only intermittantly. This represents a more severe case than either a conduit that never contains internal water or a conduit that always contains internal water at design pressure.



Loads on Rectangular Conduits

Loads on conduits are of two types - external loads and internal loads. For the purposes of this technical release; external loads are due to embankment material and contained water plus any surcharge water above the embankment surface and also include the dead weight effects of the conduit, internal loads are due to water within the conduit. The conduit must be designed to satisfactorily resist a number of possible loading conditions which may occur over the life of the structure.

External Loads

Loads are assumed uniformly distributed on the top slab, sidewalls, and bottom slab except for the bottom slab of conduits founded on rock. Appropriate recognition is made of the fact that actual sidewall loads are trapezoidal and may vary from nearly triangular to nearly uniform distributions.

Conduits on earth foundations. - Load combinations producing the maximum requirements for concrete thicknesses, steel areas, and bond should be used in design. Qualitative influence lines may be employed to help ascertain these critical load combinations. The ordinates of an influence line give the value of some function at a specific location caused by a unit load anywhere on the structure. Thus an influence line may (a) suggest theoretical loading patterns, (b) verify the inclusion of various load combinations, and (c) indicate the load combination producing the maximum value of a function.

The three influence lines for M_A , M_B , and M_C in Appendix A (see Figure 9 for location of sections A, B, and C) show that three load combinations must be considered in the design of rectangular conduits on earth. These three load combinations are designated as IC#1, IC#2, and IC#3. They are shown in Figure 2. IC#1 and IC#2 have been defined on pages 1 and 2. If p_{V1} , p_{h1} , p_{v2} , and p_{h2} are the vertical and horizontal external unit loads exclusive of conduit dead weight effects, then by those definitions

$$p_{v_1} \ge p_{v_2}$$
 and $p_{h_2} \ge p_{h_1}$

IC#3 has simultaneously high vertical and lateral pressures. This load combination is not usually of concern in the design of circular or other curved conduits but it should be considered for rectangular conduits since it causes large negative corner moments. For this work, IC#3 is taken as

$$p_{vs} = p_{v1}$$
 and $p_{hs} = p_{hs}$

Appendix B indicates one situation in which four load combinations may exist at various times. In this situation, IC#1 would correspond to developed condition - moist, while IC#2 would correspond to initial condition - saturated.

Conduits on rock foundations. - Many suggestions are made concerning the distribution of loads on the bottom slabs of conduits founded on rock. One of the common proposals is that the load should be assumed to vary linearly from zero at midspan to a maximum value at the supports. The limit of this approach is to assume the bottom load is concentrated at the sidewalls and the bottom slab itself is not loaded. Although this assumption may sound severe, it actually is not much more so than the assumption of linearity since moments in a span are largely produced by that part of the load near the central portion of the span. Thus three additional load combinations exist, they are designated IC#4, IC#5, and IC#6 and are shown in Figure 2. The latter three load combinations are the same as the former three except that they have no vertical pressure on the bottom slab.

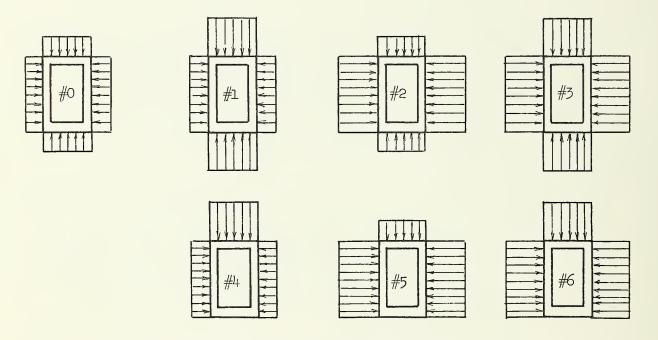


Figure 2. Load combinations producing maximum values at critical locations.

When conduits are founded on rock, the conduits must be able to safely resist all six load combinations since the actual contact and interaction with the rock is unknown. When conduits have large clear spans and are founded on rock, it may be more economical to use a fixed ended frame rather than the closed rectangular shape.

Internal Water Loads

Internal water loads should be considered in the design of rectangular pressure conduits. Although internal water loads will seldom drastically affect the design, they will always in pressure conduits cause either an increase in concrete thickness, or an increase in the theoretical amount of tension steel required at some section, or both. Internal water load may be handled conveniently by treating it as two distinct loadings

(1) Water to top of conduit, filling the conduit, but not under

pressure, and

(2) Loading due to pressure head, h_{W} , above the bottom of the top slab.

The first loading amounts to hydrostatic loading on the sidewalls only since load and reaction on the bottom slab cancel each other.

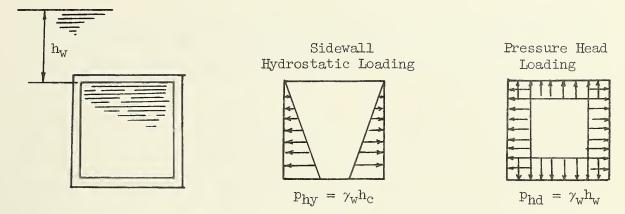


Figure 3. Treatment of internal water loads.

The second loading creates a uniform distribution all around. The magnitude of h_W may be related in some way to the height of embankment over the conduit, it is taken therefore as a function of p_{V2} , or

$$h_{W} = \frac{1}{2} (\frac{p_{V2}}{100})$$

where p_{v2} is in psf and h_{w} is in ft.

Sketches of the deflected shape of the conduit caused by the hydrostatic loading show that moments at the midspans are positive (tension on the inside of the conduit) for the top and bottom slabs and are negative (tension on outside of the conduit) for the sidewalls. However, deflected shapes caused by the pressure head loading show that midspan moments in any span may take on either sign depending on the proportions of the conduit. It is apparent that moments due to internal water loads are additive to some of the moments of interest due to the external loads.

Basic Sets of Loads

Hence, when a conduit is to carry internal water, there are three basic sets of loads which should be considered to determine the critical combination of loads for each function investigated. These basic sets are identified as

(Bl) External loads only, conduit empty

(B2) External loads plus internal water loads when conduit is flowing full as an open channel, and

(B3) External loads plus internal water loads when conduit is flowing full under pressure head, $h_{\rm w}$.

Therefore, the problem is to determine which external load combination should be combined with which internal load, if any, to produce the maximum effect for each function. The internal loading is either the sidewall hydrostatic loading or the sidewall hydrostatic loading plus the pressure head loading.

LC#0, shown in Figure 2, is included to take care of those cases for which it is desirable to consider minimum external loads in combination with internal water loads. For this work, LC#0 is taken as

$$p_{VO} = p_{V2}$$
 and $p_{ho} = p_{h1}$

Method of Analysis for Indeterminate Moments

General Considerations

Slope Deflection is selected as the method of analysis for use in this work because the method yields explicit solutions. Although Moment Distribution in some instances yields exact solutions, in general it is a method of successive approximations which is summed after some finite number of cycles of distribution are performed. Hence, where a large number of solutions are required, an explicit method of analysis has an advantage over a method requiring iterative procedures.

In accordance with usual theory, the analysis assumes straight-line stress distribution on a cross section. This assumption is less well satisfied as the thickness-to-span ratio increases. For thick members, the effect of shearing strains is important.

Members are assumed non-prismatic having a constant moment of inertia within the clear span and having moments of inertia which approach infinity outside the clear span. This assumption, when used with the sidewalls, introduces approximations discussed below. Figure 4 shows this variation in moments of inertia.

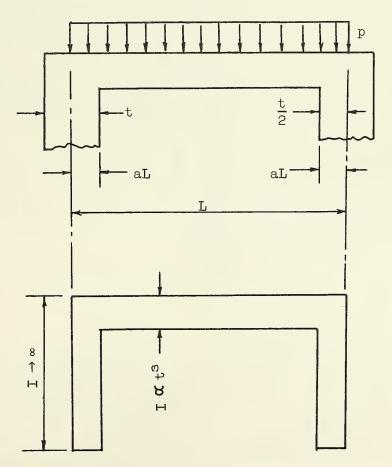


Figure 4. Assumed variation in moment of inertia.

Dissymmetry of Sidewalls

See Figure 5 which identifies the nomenclature concerning spans and member thicknesses. The conduit lacks symmetry of shape about any horizontal axis because of two inequalities. These are

$$t_b > t_t$$
 $t_{sb} > t_{st}$

Both inequalities cause the sidewalls to lack symmetry and therefore cause the sidewall stiffnesses, carry over factors and fixed end moments to be different at the top and bottom of the sidewalls. Final moments and shears are affected to some extent. Two questions arise; first, how serious is the effect and second, how should the sidewall be treated?

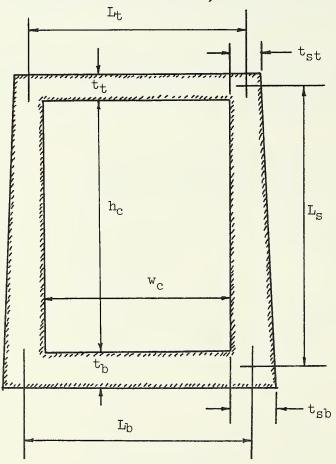


Figure 5. Conduit spans and member thicknesses.

Some insight into the effect of this lack of symmetry of shape on the final moments may be obtained by considering the effect of varying the stiffnesses of either the tops of the sidewalls or the bottoms of the sidewalls. Note that both inequalities produce the same sort of result since both represent, as compared to equality situations, a decrease in stiffness of the tops and an increase in stiffness of the bottoms of the sidewalls.

Consideration that $t_b \ge (t_t+1)$. - The bottom slab thickness will exceed the top slab thickness because the bottom slab carries a slightly larger dead load than the top slab and the bottom slab has 1 inch more concrete cover over the outside steel than does the top slab. The

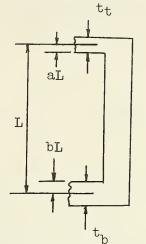


Figure 6. Unequal slab thicknesses.

importance of this inequality may be evaluated qualitatively by observing Figures 29-31 on pages 152-154 in "Continuous Frames of Reinforced Concrete" by Cross and Morgan where $aL = \frac{1}{2}(t_t)$,

 $bL = \frac{1}{2}(t_b)$, and $L = h_c + \frac{1}{2}(t_t + t_b)$. These charts can be used to obtain stiffnesses and carry over factors for various a and b values. Values of fixed end moments can be computed by statics knowing

$$M_{L'}^F = \frac{1}{12}p(L')^2$$
 where $L' = L - aL - bL$.

Note that tb will not differ from tt by more than a few inches at most. It seems clear that the effect of this inequality can

not be great within the existing limits of relative values of $t_{
m b}$ and $t_{
m t}.$ Thus it is concluded, it is not necessary to make the refinement that tb # tt. To obtain values for design use

$$aL = bL = \frac{1}{4}(t_{t}+t_{b}).$$

Consideration that $t_{\rm sb} > t_{\rm st}.$ - The thickness of the sidewall increases in a downward direction because of the necessity of providing batter on

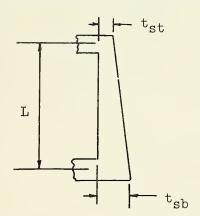


Figure 7. Sidewall batter.

the outside surfaces of the walls. The importance of this inequality may be evaluated qualitatively by observing Figure 27 on page 150 of Cross and Morgan or by observing Charts 2 and 3 on pages 258 and 259 in "Statically Indeterminate Structures" by Anderson. The source of these charts is noted as the Portland Cement Association, they can be found in several texts. The parameters of interest can be obtained from the right hand sides of the pairs of Graphs 1, 2, and 3. Note that t_{sb} and t_{st} are not greatly different within the clear height of the sidewall since the batter is about 3/8 inch per foot. Thus it is con-

cluded, it is not necessary to make the refinement that $t_{sb} \neq t_{st}$. obtain values for design assume the thickness of the sidewall is constant and use

 $t_s = \frac{1}{2}(t_{st} + t_{sb})$

Slope Deflection Equation

The Slope Deflection Equation used in this analysis is derived for the assumption that members are symmetrical about their centerlines and are subjected to applied loads and end rotations only. That is, members do not undergo relative translation of their ends. The usual Slope Deflection sign convention is followed; clockwise rotations are positive, clockwise joint moments are positive.

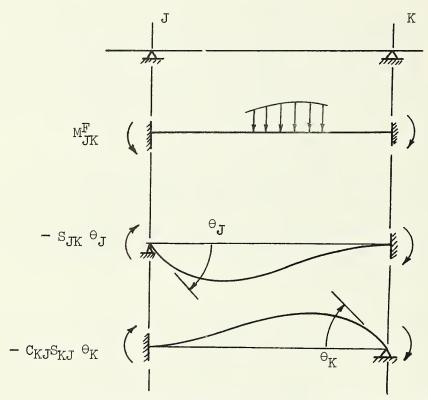


Figure 8. Development of Slope Deflection Equation.

From Figure 8

$$\mathtt{M}_{JK} \; = \; \mathtt{M}^{F}_{JK} \; \boldsymbol{\mathsf{-}} \; \mathtt{S}_{JK} \; \; \boldsymbol{\boldsymbol{\theta}}_{J} \; \boldsymbol{\mathsf{-}} \; \mathtt{C}_{KJ} \; \; \mathtt{S}_{KJ} \; \; \boldsymbol{\boldsymbol{\boldsymbol{\theta}}}_{K}$$

and similarly

$$\mathbf{M}_{KJ} \ = \ \mathbf{M}_{KJ}^F \ \textbf{-} \ \mathbf{S}_{KJ} \ \boldsymbol{\theta}_K \ \textbf{-} \ \mathbf{C}_{JK} \ \mathbf{S}_{JK} \ \boldsymbol{\theta}_J$$

however, due to symmetry

$$S_{JK} = S_{KJ} = S$$
 and $C_{JK} = C_{KJ} = C$

then

$$M_{JK} = M_{JK}^F - S(\Theta_J + C\Theta_K)$$

$$\mathbf{M}_{\mathrm{KJ}} = \mathbf{M}_{\mathrm{KJ}}^{\mathrm{F}} - \mathbf{S}(\mathbf{\Theta}_{\mathrm{K}} + \mathbf{C}\mathbf{\Theta}_{\mathrm{J}})$$

where

 ${\rm M_{JK}}$ is the moment at J in span JK ${\rm M_{KJ}}$ is the moment at K in span JK ${\rm M_{\tilde{f}_{JK}}}$ is the fixed end moment at J in span JK ${\rm M_{\tilde{f}_{KJ}}^F}$ is the fixed end moment at K in span JK ${\rm S_{JK}}$ is the stiffness at end J in span JK ${\rm S_{KJ}}$ is the stiffness at end K in span JK ${\rm C_{JK}}$ is the stiffness at end K in span JK ${\rm C_{JK}}$ is the carry over factor from end J to end K ${\rm C_{KJ}}$ is the carry over factor from end K to end J $\theta_{\rm J}$ is the end rotation at support J $\theta_{\rm K}$ is the end rotation at support K

Slope Deflection Method

Both the loading on, and the shape of, these single cell rectangular conduits are symmetrical about the vertical centerline of the structure. Hence no joint can translate. There are two unknown displacements, say

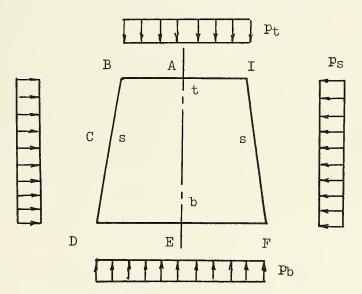


Figure 9. Designations for analyses.

the two rotations θ_B and θ_D since by symmetry $\theta_I = -\theta_B$ and $\theta_F = -\theta_D$. Two joint (statical moment) equations are required to determine these rotations. Say

$$\Sigma M_{B} = M_{BI} + M_{BD} = 0$$

$$\Sigma M_{D} = M_{DB} + M_{DF} = 0$$

By the Slope Deflection Equations:

$$M_{BI} = M_{BI}^{F} - S_{t}(1 - C_{t})\Theta_{B}$$

$$M_{BD} = M_{BD}^{F} - S_{s}(\Theta_{B} + C_{s}\Theta_{D})$$

and

$$M_{DB} = M_{DB}^{F} - S_s(\theta_D + C_s\theta_B)$$

$$M_{DF} = M_{DF}^{F} - S_b(1 - C_b)\theta_D$$

These expressions for moment may be substituted in the joint equations from which θ_B and θ_D may be determined. The values of θ_B and θ_D can then be inserted in the Slope Deflection Equations yielding for the

general case assumed herein:

$$\begin{aligned} \mathbf{M}_{\mathrm{BI}} &= \mathbf{M}_{\mathrm{BI}}^{\mathrm{F}} - \mathbf{S}_{\mathrm{t}} (1 - \mathbf{C}_{\mathrm{t}}) \begin{bmatrix} \left\{ (1 - \mathbf{C}_{\mathrm{b}}) \mathbf{S}_{\mathrm{b}} + \mathbf{S}_{\mathrm{s}} \right\} (\mathbf{M}_{\mathrm{BI}}^{\mathrm{F}} + \mathbf{M}_{\mathrm{BD}}^{\mathrm{F}}) - \mathbf{C}_{\mathrm{s}} \mathbf{S}_{\mathrm{s}} (\mathbf{M}_{\mathrm{DB}}^{\mathrm{F}} + \mathbf{M}_{\mathrm{DF}}^{\mathrm{F}}) \\ \left\{ (1 - \mathbf{C}_{\mathrm{t}}) \mathbf{S}_{\mathrm{t}} + \mathbf{S}_{\mathrm{s}} \right\} \left\{ (1 - \mathbf{C}_{\mathrm{b}}) \mathbf{S}_{\mathrm{b}} + \mathbf{S}_{\mathrm{s}} \right\} - (\mathbf{C}_{\mathrm{s}} \mathbf{S}_{\mathrm{s}})^{2} \end{aligned} \right]^{\mathrm{nd}} \\ \mathbf{M}_{\mathrm{DF}} &= \mathbf{M}_{\mathrm{DF}}^{\mathrm{F}} - \mathbf{S}_{\mathrm{b}} (1 - \mathbf{C}_{\mathrm{b}}) \begin{bmatrix} \left\{ (1 - \mathbf{C}_{\mathrm{t}}) \mathbf{S}_{\mathrm{t}} + \mathbf{S}_{\mathrm{s}} \right\} (\mathbf{M}_{\mathrm{DB}}^{\mathrm{F}} + \mathbf{M}_{\mathrm{DF}}^{\mathrm{F}}) - \mathbf{C}_{\mathrm{s}} \mathbf{S}_{\mathrm{s}} (\mathbf{M}_{\mathrm{BI}}^{\mathrm{F}} + \mathbf{M}_{\mathrm{BD}}^{\mathrm{F}}) \\ \left\{ (1 - \mathbf{C}_{\mathrm{t}}) \mathbf{S}_{\mathrm{t}} + \mathbf{S}_{\mathrm{s}} \right\} \left\{ (1 - \mathbf{C}_{\mathrm{b}}) \mathbf{S}_{\mathrm{b}} + \mathbf{S}_{\mathrm{s}} \right\} - (\mathbf{C}_{\mathrm{s}} \mathbf{S}_{\mathrm{s}})^{2} \end{aligned}$$

also

$$M_{\mathrm{BD}} = - M_{\mathrm{BI}}$$

$$\mathrm{M}_{\mathrm{DF}} = - \mathrm{M}_{\mathrm{DB}}$$

The various fixed end moments, stiffnesses, and carry over factors involved may be computed from the relations

Fixed end moment =
$$M_i^F = m_i^F p_i L_i^2$$

Stiffness =
$$S_i = k_i EI_i/L_i \alpha k_i t_i^3/L_i$$

Carry over factor = Ci

The coefficients m_i , k_i , and C_i may be obtained from Table 2-5, page 2-9 of Technical Release No. 30, or from the expressions

$$m_{i}^{F} = \frac{1}{12}(1 + 2a - 2a^{2})$$

$$k_i = \frac{1}{(1-2a)\left\{1-\frac{3}{4(1-a+a^2)}\right\}}$$

$$C_i = \frac{3}{2(1-a+a^2)} - 1$$

where (a) is defined in Figure 4

In the analysis, take for top slab, sidewall, and bottom slab respectively:

$$L_{t} = w_{c} + t_{st} \qquad a_{t}L_{t} = \frac{1}{2} t_{st} \qquad t_{t} = t_{t}$$

$$L_{s} = h_{c} + \frac{1}{2}(t_{t} + t_{b}) \qquad a_{s}L_{s} = \frac{1}{4}(t_{t} + t_{b}) \qquad t_{s} = \frac{1}{2}(t_{st} + t_{sb})$$

$$L_{b} = w_{c} + t_{sb} \qquad a_{b}L_{b} = \frac{1}{2} t_{sb} \qquad t_{b} = t_{b}$$

The resultant expressions for $\rm M_{BI}$ and $\rm M_{DF}$ may be checked against known solutions for special cases, for instance $\rm M_{K}$ in Tables 2-4 and 2-6 of Technical Release No. 30, also $\rm M_{ab}$ and $\rm M_{dc}$ in ES-28.

Design Criteria

Materials

Class 4000 concrete and intermediate grade steel are assumed.

Working Stress Design

Design of sections is in accordance with working stress methods. allowable stresses in psi are

Extreme fiber stress in flexure	$f_c = 1600$
Shear, V/bd at (d) from face of support *	v = 70
Flexural Bond	
tension top bars	$u = 3.4\sqrt{f_c'}/D$
	1 0 1 -

other tension bars
$$u = 4.8\sqrt{f_c'}/D$$

Steel

in tension					= 20,000
in compression,	axially	loaded	columns	f_s	= 16,000

Minimum Slab Thicknesses

Top slab and	10	inches
Bottom slab	11	inches

Sidewall Batter

Approximately 3/8 in per foot, using whole inches for sidewall thicknesses at top and bottom of the sidewall.

Temperature and Shrinkage Steel

The minimum steel ratios are

for outside faces	$p_t = 0.001$
for inside faces	$p_{t} = 0.002$

Slabs more than 32 inches thick are taken as 32 inches.

Web Reinforcement

The necessity of providing some type of stirrup or tie in the slabs because of bending action is avoided by

- (1) limiting the shear stress, as a measure of diagonal tension, so that web steel is not required, and
- (2) providing sufficient effective depth of sections so that compression steel is not required for bending.

Cover for Reinforcement

Steel cover is everywhere 2 inches except for outside steel in the bottom slab where cover is 3 inches.

Spacing of Reinforcement

The maximum permissible spacing of any reinforcement is 18 inches.

^{*}In some cases shear may be critical at the face of the support, see page 17.

Slab Thicknesses Required by Shear

Consideration of various influence lines for shear at the faces of supports indicate that with the exception of shear in the sidewalls of conduits on rock, shear thickness design of a particular slab may be performed assuming the slab is a simple span. This is obviously true of top and bottom slabs due to symmetry of load and shape of the structure about the vertical centerline of the structure. It is an approximation when applied to sidewall design since the corner moments at top and bottom are in general unequal. The moments are unequal because neither the loads nor the shape of the structure is symmetrical about any horizontal line.

Location of Critical Sections for Shear

In ordinary beams and slabs the shear within distance (d) from the face of a support is less critical than that at the distance (d) from the support. The ACI Code therefore stipulates critical shear as that located a distance (d) from the support. However, with reaction conditions as illustrated in sketch (b) of Figure 10, diagonal tension cracking can take place at the face of the support. Computation of critical shear at distance (d) does not apply in such cases, critical shear is located at the face of the support.

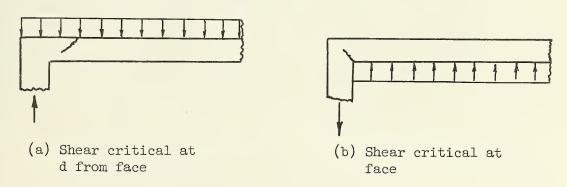


Figure 10. Location of critical shear.

When internal water loads are included in the design of rectangular conduits, required shear thickness is sometimes controlled by shear at the face of the support.

Design of Top Slab

The top slab of a pressure conduit is subject to two possible controlling loads as shown in Figure 11.

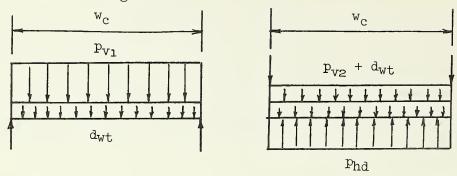


Figure 11. Loads for shear thickness design of top slab.

Shear in the top slab depends on the dead weight of the slab. The dead weight depends on the thickness which is initially unknown. Hence a convergence procedure is desirable. The larger of the two computed thicknesses controls.

$$t_t = d + 2.5$$

 $d_{wt} = 150t_t/12$

from the first loading, shear critical at distance (d)

$$v = \frac{\frac{1}{2}(p_{V1} + d_{Wt})w_{c} - (p_{V1} + d_{Wt})d/12}{bd}$$

or

$$t_{t} = \frac{\frac{1}{2}(p_{v1} + d_{wt})w_{c}}{840 + (p_{v1} + d_{wt})/12} + 2.5$$

from the second loading, shear critical at face

$$t_{t} = \frac{\frac{1}{2}(p_{hd} - p_{v2} - d_{wt})w_{c}}{840} + 2.5$$

If $(p_{hd} - p_{v2} - d_{wt}) < 0$, the second shear does not exist. In these relations

p_{v1} = vertical unit load of LC#1, in psf

 p_{v2} = vertical unit load of IC#2, in psf

 $p_{hd} = \gamma_w h_w = 62.4 h_w$, in psf

 $d_{\text{Wt}} = \text{dead weight of top slab, in psf}$

 w_c = clear width of conduit, in ft

b = 12 inches

d = effective depth, in inches

 t_t = thickness of top slab, in inches

v = allowable shear stress = 70 psi

Design of Sidewall

The sidewall design for required shear thickness is more complex than that of the top slab. Several problems need consideration, among these are

- (1) sidewall loads are trapezoidal,
- (2) sidewall thickness increases with depth,
- (3) critical sidewall shear for conduits on rock is usually a function of the maximum external loads on the top slab, and
- (4) internal water loads for pressure conduits may produce critical sidewall shear at either the face of the top support or the face of the bottom support.

Conduits founded on earth, without internal water loads. - This case is the simplest to design. As previously noted, the actual external lateral loads are trapezoidal ranging from nearly triangular for conduits near the surface to nearly uniform for conduits at great depth. What is needed is some way of conservatively approximating the shear diagram over those portions of it that may be critical.

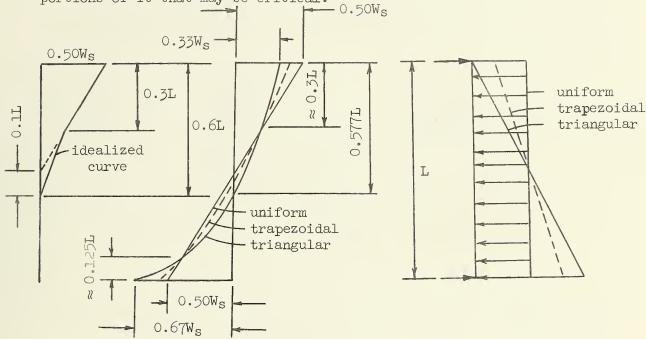


Figure 12. Load distributions and shear diagrams for same total lateral load, W_s.

Figure 12 shows that the assumption of a uniform load gives conservative shear values between 0.0L and 0.3L from the top and between 0.125L and 0.5L from the bottom. Usually conservative shear values between 0.3L and 0.6L from the top may be obtained by using the idealized curve indicated. Recalling that shear stress is critical at (d) from the face of a support, then shear between 0.0L and 0.125L from the bottom will never be critical for all but perhaps those conduits having very large clear heights and small loads. Further, since sidewall thicknesses over the lower half of the sidewall are greater than over the upper half, sidewall thickness will not be controlled by shear between 0.125L and 0.5L from the bottom.

The following procedure for determining the sidewall thickness for the conduits therefore applies. Compute the required effective depth on the assumption of a uniformly loaded simple span loaded with p_{h2} . If the critical section at (d) from the face of the top support, is more than 0.3L from the top, recompute the required effective depth on the basis of the idealized curve. With (d) known compute the sidewall thickness at the top, t_{st} , and the sidewall thickness at the bottom, t_{sb} , taking into account the required batter. Equations for these computations are given below in combination with requirements for conduits on rock.

Conduits founded on rock, without internal water loads. - The influence line for shear V_B in the sidewall, given in Appendix A, shows that loads on the top slab produce the same kind of shear at the top of the sidewall as does the sidewall loading, however loads on the bottom slab produce the opposite kind of shear. When conduits are on rock, loads on the top slab are possible when the bottom slab is not loaded. Thus LC#6 produces the maximum shear at the top of the sidewall. This conclusion is verified by Figure 13 which shows the deflected shape and sense of end moments on the sidewall due to loading on the top slab. These end moments produce an extra shear which adds to that due to the sidewall loads.

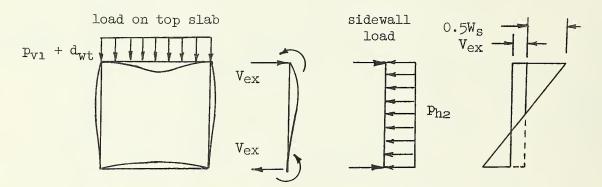


Figure 13. Sidewall shear, conduits on rock foundation.

This extra shear, $V_{\rm ex}$, can be added to the shear diagram for sidewall loads and the procedures given above for conduits on earth foundations may be followed. Figure 14 shows a portion of this combined shear diagram rotated 90 degrees.

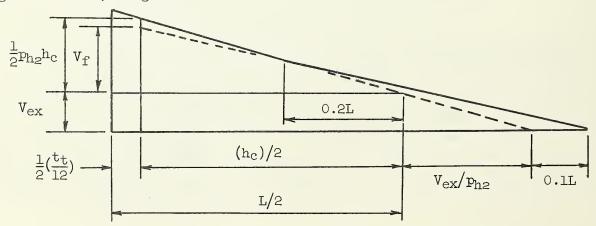


Figure 14. Partial sidewall shear diagram.

Assuming the critical section for shear is not more than 0.3L from the top (left end), then

$$v = \frac{\frac{1}{2} p_{h2} h_c + V_{ex} - p_{h2} d_{st}/12}{bd_{st}}$$

or

$$d_{\text{St}} = \frac{\frac{1}{2} p_{\text{h2}} h_{\text{c}} + V_{\text{ex}}}{8 h_{\text{0}} + p_{\text{h2}}/12}$$

However, if the critical section is more than 0.3L from the top, that is, if

$$(\frac{1}{2}t_t + d_{st})/12 > 0.3(\frac{t_t}{12} + h_c)$$

then get the new shear at the face of the support, which is

$$V_{f} + V_{ex} = \left\{ \left(\frac{1}{2} p_{h2} h_{c} \right) \left(\frac{0.2L}{h_{c}/2} \right) + V_{ex} \right\} \left\{ \frac{\frac{1}{2} h_{c} + V_{ex}/p_{h2} + 0.1L}{0.3L + V_{ex}/p_{h2}} \right\}$$

divide this by $(\frac{1}{2}h_c + V_{ex}/p_{h2} + 0.1L)$ to obtain the new effective unit load. The required effective depth becomes

$$d_{\text{st}} = \frac{v_{\text{f + }}v_{\text{ex}}}{840 + (\frac{1}{2}h_{\text{c}} + v_{\text{ex}}/p_{\text{h2}} + 0.1L})/12}$$

where $V_{\rm ex}$ = extra shear from top slab load, in lbs

 V_f = shear at face from idealized curve, in lbs

 $L = h_c + t_t/12$, in ft

 h_c = clear height of conduit, in ft

d_{st} = effective depth of sidewall at d_{st} from top, in inches

These expressions may be used for conduits on earth, in which case $V_{\rm ex}$ is equal to zero, or for conduits on rock.

Convergence procedure - conduits on rock. - When conduits are on rock, the correct value for $V_{\rm ex}$ is initially unknown since it depends on the sidewall end moments due to loading on the top slab. These end moments are obtained from indeterminate analyses which are functions of the thicknesses and span lengths of all members, quantities which are in the process of being determined. Thus a convergence approach to design is required here. The initial value of $V_{\rm ex}$ is set at zero. Then the remaining shear design is completed. Indeterminate analyses are performed and the end moments due to top loads obtained. If $M_{\rm But}$ and $M_{\rm Dut}$, see page 27, are the moments in ft-lbs at B and D due to a uniform load of unity on the top slab, then $V_{\rm ex}$ is given by

$$V_{\text{ex}} = (p_{\text{vl}} + d_{\text{wt}})(M_{\text{But}} + M_{\text{Dut}})/(h_{\text{c}} + \frac{1}{2}(t_{\text{t}} + t_{\text{b}})/12)$$

This furnishes a new value for $V_{\rm ex}$ which may be used in the expressions for effective depth, $d_{\rm st}$. Then the remaining shear design is completed and the cycle is repeated as many times as is necessary. The process is ended when the required sidewall thickness is unchanged from one cycle to the next.

Limit of shear criteria. - A further complication may exist when the sidewall shear includes $V_{\rm ex} > 0$. According to the ACI Code, critical

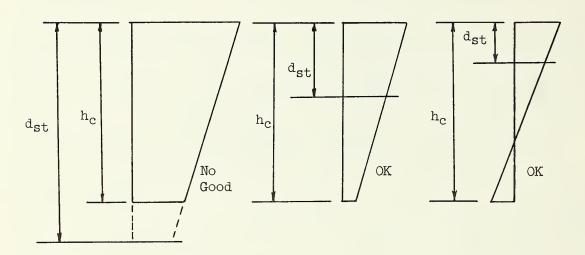


Figure 15. Possible sidewall shear diagrams with Vex included.

sections for shear are located (d) from the face of the support. As indicated in Figure 15 it is possible for the computed value of $d_{\rm st}$ to locate the critical section outside of the span, $h_{\rm c}$. If this occurs, the shear criteria is held invalid and the design is terminated.

Conduits with internal water loads. - The sidewall thickness of pressure conduits may be determined by internal water loads rather than by maximum external load combinations. Further it is not known beforehand whether shear at the top or shear at the bottom of the sidewall will control.

At the top, maximum shear due to internal water load occurs, if it exists, when the external loading on the sidewall is a minimum. This can be taken as IC#1. At the bottom, maximum shear due to internal water load occurs, if it exists, when the external loading on the sidewall is a minimum, the external loading on the top slab is a maximum, and the external loading on the bottom slab is a minimum. This is IC#4 for conduits on rock and can be taken as IC#1 for conduits on earth. Note that $V_{\rm ex}$ in this case adds to the shear at the bottom.

For these computations, since p_{h1} is of secondary importance here, it is treated strictly as a uniform load with no adjustment made for a trapezoidal distribution.

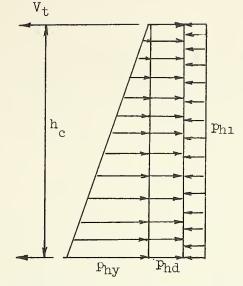


Figure 16. Loading for sidewall thickness, control from top.

so

$$V_t = \frac{1}{2}(p_{hd} - p_{h1})h_c + \frac{1}{3}(\frac{1}{2}p_{hy})h_c$$

and the shear stress at the top face is

$$v = V_t/bd_{st}$$

giving

$$d_{st} = V_t/840.$$

where

 V_{\pm} \approx shear at top face, in lbs

$$p_{hy} = \gamma_w h_c = 62.4 h_c$$
, in psf

 d_{St} = effective depth of sidewall at top face, in inches

If $V_t < 0$ the desired shear does not exist.

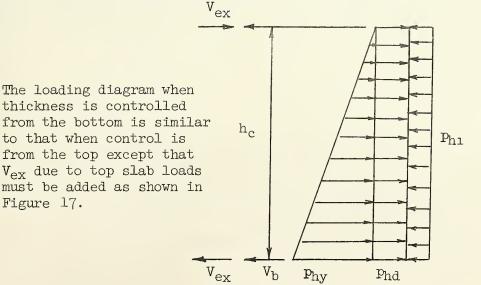


Figure 17. Loading for sidewall thickness, control from bottom.

$$V_b = \frac{1}{2}(p_{hd} - p_{h1})h_c + \frac{2}{3}(\frac{1}{2}p_{hy})h_c$$

and the shear stress at the bottom face is

$$v = (V_b + V_{ex})/bd_{sb}$$

giving

$$d_{sb} = (V_b + V_{ex})/840.$$

where

 V_h \approx shear at bottom face, in lbs

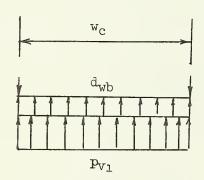
 d_{Sb} = effective depth of sidewall at bottom face, in inches

If $V_b < 0$ the desired shear can not control.

Summary, shear design of sidewall thickness. - In the general case the thickness of the sidewall may be governed at the top by external loads, at the top with internal water loads, or at the bottom with internal water loads. In the first and last instances extra shear must be added for conduits on rock. The actual thickness required at the top of the sidewall, $t_{\rm st}$, and the corresponding actual thickness required at the bottom of the sidewall, $t_{\rm sb}$, is selected from the most critical set of thicknesses determined from the two computed values of $d_{\rm st}$ and the one value of $d_{\rm sb}$.

Design of Bottom Slab

The bottom slab of a pressure conduit is subject to two possible controlling loads as shown in Figure 18



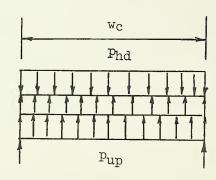


Figure 18. Loads for shear thickness of bottom slab.

The bottom slab may carry the dead weight of the top slab and the sidewalls. Since $t_{\rm b}$ is as yet unknown, take $t_{\rm h}$ = $t_{\rm t}$ + 1, so

$$d_{wb} = \frac{150 \left\{ w_c t_t + (h_c + (2t_t + 1)/12)(t_{st} + t_{sb}) \right\} / 12}{w_c + 2t_{sb}/12}$$

For the first loading, shear critical at distance (d)

$$t_b = d + 3.5$$

$$t_b = \frac{\frac{1}{2}(p_{v1} + d_{wb})w_c}{840 + (p_{v1} + d_{wb})/12} + 3.5$$

For the second loading, if the conduit is on earth $p_{up} = p_{v2} + d_{wb}$, if the conduit is on rock $p_{up} = 0$, therefore

$$t_b = d + 2.5$$

and, with shear critical at face

$$t_b = \frac{\frac{1}{2}(p_{hd} - p_{up})w_c}{840} + 2.5$$

where

 d_{Wb} = dead weight on bottom slab, in psf

 t_b = thickness of bottom slab, in inches

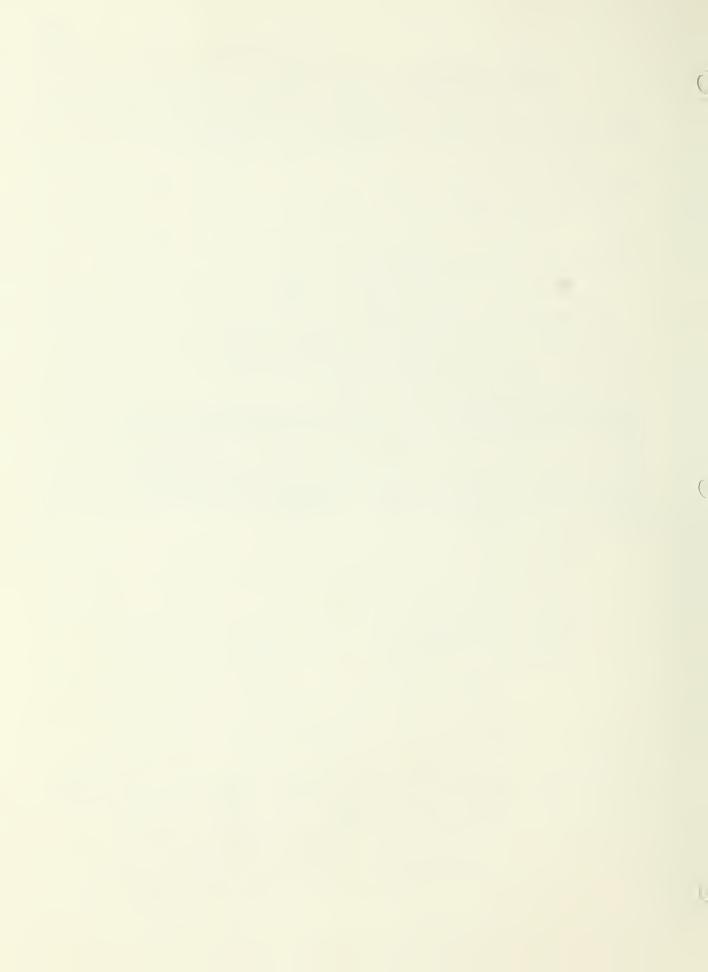
d = effective depth, in inches

If $(p_{hd} - p_{up}) < 0$, the desired shear does not exist.

The larger of the two computed thicknesses controls.

Summary of Shear Design

The set of thicknesses t_t , t_{st} , t_{sb} , and t_b just obtained represents the minimum possible slab thicknesses consistent with the selected criteria for shear as a measure of diagonal tension. This set is the first trial set of thicknesses for which indeterminate analyses can be made and subsequent determinations of required steel areas can be obtained. It may be found necessary to increase one or more of these thicknesses in subsequent stages of the design.



Analyses of Corner Moments

With all conduit dimensions known, indeterminate analyses for moments can be performed. Before this is done, it is desirable that all unit loads on top, sides, and bottom slabs be evaluated for the seven load combinations previously established. these are

for which,

$$d_{wb} = \frac{150 \left\{ w_c t_t + (h_c + (t_t + t_b)/12)(t_{st} + t_{sb}) \right\} / 12}{w_c + 2t_{sb}/12}$$

Unit Load Analyses

Corner moments for seven external load combinations and two internal water loadings are required. Rather than perform these nine analyses, three unit load analyses, with the magnitudes of the unit load taken as unity, may be used to obtain corner moments for all but one of the internal water loadings. The analyses needed are shown in Figure 19

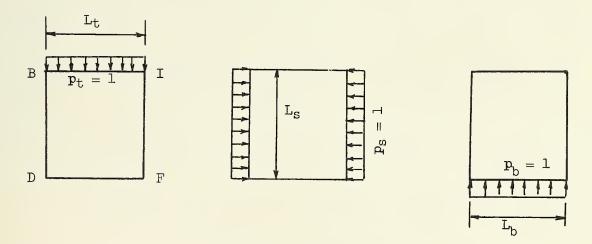


Figure 19. Loadings for unit load analyses.

The corner moments at B and D for each of the three unit loadings may be obtained from the general solutions for $M_{\rm BI}$ and $M_{\rm DF}$ previously derived. These moments in ft-lbs per lb of loading, are designated $M_{\rm But}$, $M_{\rm Dut}$, $M_{\rm Bus}$, $M_{\rm Dus}$, $M_{\rm Bub}$, and $M_{\rm Dub}$ respectively. Immediately after $M_{\rm But}$ and $M_{\rm Dut}$ are obtained, a revised estimate of $V_{\rm ex}$ may be

computed when necessary as discussed on page 21.

Evaluation of External Load Corner Moments

Corner moments for a given load combination may be obtained as the sums of the respective unit load moments times the corresponding actual external loads. Thus, adopting the nomenclature $M_{\rm Bi}=M_{\rm BIi}$ and $M_{\rm Di}=M_{\rm DFi}$, where $M_{\rm B}$ and $M_{\rm D}$ take on the same Slope Deflection signs as $M_{\rm BI}$ and $M_{\rm DF}$ the moments in ft-lbs are

$$M_{\text{Bi}} = p_{\text{ti}} M_{\text{But}} + p_{\text{si}} M_{\text{Bus}} + p_{\text{bi}} M_{\text{Bub}}$$

$$M_{\text{Di}} = p_{\text{ti}} M_{\text{Dut}} + p_{\text{si}} M_{\text{Dus}} + p_{\text{bi}} M_{\text{Dub}}$$

$$i = 0,1,2,3,4,5,6$$

Referring to the discussions on pages 10 and 11, note that the assumptions relating to sidewalls

(1)
$$aL = bL = 1/4(t_b + t_t)$$
 for $t_b > t_t$

(2)
$$t_s = 1/2(t_{sb} + t_{st})$$
 for $t_{sb} > t_{st}$

as well as the assumption

(3) sidewall loading is uniform instead of trapezoidal

may all cause the corner moments at B to be computed too high and the corner moments at D to be computed too low. That is, the errors may be additive and on the safe or unsafe side depending on the moment or other function under consideration. Therefore to partially account for the effects of the three assumptions, a second set of corner moments is computed in which the moments due to side loads are arbitrarily adjusted 10 percent. Now

$$M_{\text{Bi}} = p_{\text{ti}}M_{\text{But}} + 0.9p_{\text{si}}M_{\text{Bus}} + p_{\text{bi}}M_{\text{Bub}}$$

$$M_{\text{Di}} = p_{\text{ti}}M_{\text{Dut}} + 1.1p_{\text{si}}M_{\text{Dus}} + p_{\text{bi}}M_{\text{Dub}}$$

$$i = 0,1,2,3,4,5,6$$

This second set of external load corner moments is used only in those instances when it is conservative to take a lower moment at B or a higher moment at D.

Analyses for Internal Water Loads

Moments due to pressure head loading may be computed using the unit load analyses

$$M_{Bhd} = - p_{hd}(M_{But} + M_{Bus} + M_{Bub})$$

 $M_{Dhd} = - p_{hd}(M_{Dut} + M_{Dus} + M_{Dub})$

The minus signs are used since phd is an outward acting load.

Moments due to hydrostatic sidewall loading may be computed from the general solutions for $M_{
m BI}$ and $M_{
m DF}$ after the fixed end moments are obtained.

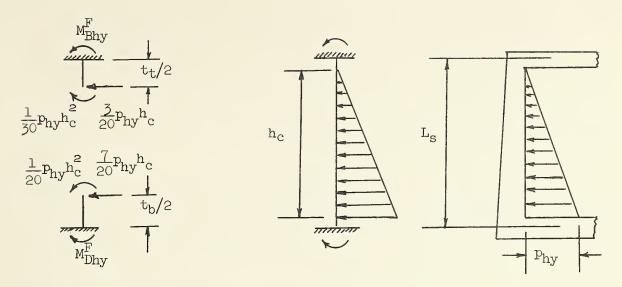


Figure 20. Fixed end moments for hydrostatic loading.

From the figure, the fixed end moments in ft-lbs are

$$M_{Bhy}^{F} = + \left(\frac{1}{30} p_{hy} h_{c}^{2} + \frac{1}{160} p_{hy} h_{c} t_{t} \right)$$

$$\mathbf{M}_{Dhy}^{F} = - \; (\; \frac{1}{20} \mathbf{P}_{hy} \mathbf{h}_{c}^{2} + \frac{7}{480} \mathbf{P}_{hy} \mathbf{h}_{c} \mathbf{t}_{b} \;)$$

where h_c is in ft and t_t and t_b are in inches.

Sense of Corner Moments

Confusion sometimes exists as to the sense of various moments. The Slope Deflection sign convention and the bending moment sign convention are independent of one another. The Slope Deflection convention is concerned with the sense of moments acting on joints (or on the ends of members). The bending moment convention is concerned with whether a moment causes tension on the inside or outside (sometimes top or bottom) of a member. Figure 21 shows the senses of various moments when the solutions for $M_{\mbox{\footnotesize{Bi}}}$ and $M_{\mbox{\footnotesize{Di}}}$ are positive in accordance with the adopted Slope Deflection convention.

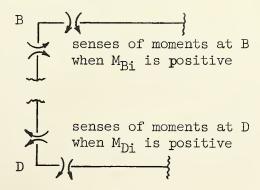
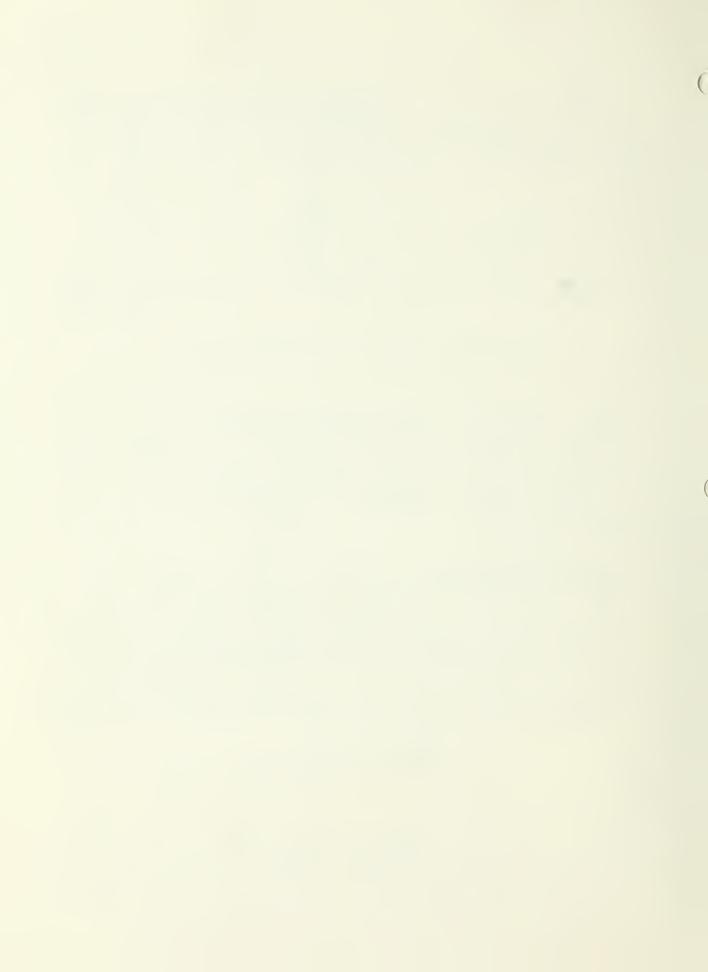


Figure 21. Sense of moments from Slope Deflection solution.



Steel Required by Combined Bending Moment and Direct Force

After slab thicknesses are known and corner moments for external and internal loads have been determined, the next step is to compute steel areas required at the fourteen locations given in Figure 1. In order to do this, there must be a procedure by which required areas may be obtained for any acceptable combination of moment and direct force. The load combination or combinations that may produce maximum required area for each design mode must also be recognized.

Treatment of Bending Moment and Direct Force

The procedure for determining required areas, to be general, must handle all cases of $M \ge 0$ and N either compression, tension, or zero. This is indicated schematically in Figure 22 which shows three statically equivalent force systems.

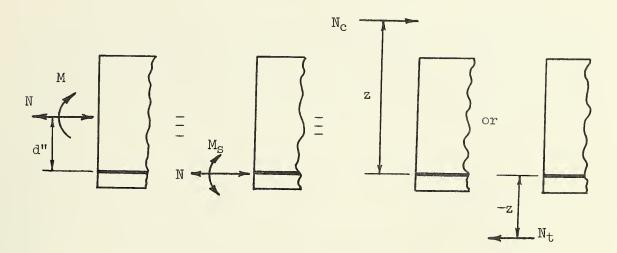


Figure 22. Range of values of moment and direct force.

Usual case, direct force at large eccentricity. - For the majority of combinations of moment and direct force, the procedure specified in National Engineering Handbook Section 6, subsection 4.2.2(c) applies and is followed. Thus, taking compressive direct force and clockwise moment in Figure 22 as positive

$$M_S = M + Nd''/12$$

and

$$12M_s = \frac{1}{2}f_ckjbd^2 = \frac{1}{2}bd^2(\frac{f_s}{n})(\frac{k}{1-k})kj$$

from which k may be determined from the cubic equation

$$-\frac{1}{3}k^3 + k^2 + kF = F$$

where

$$F = \frac{12M_s}{\frac{1}{2}bd^2(\frac{f_s}{n})}$$

then

$$A = \frac{12M_{S}}{f_{S} \text{ jd}}$$

and

$$A_{S} = A - \frac{N}{20000}$$

where M = moment about mid-depth of section in ft-lbs

 M_s = moment about tension steel, in ft-lbs

N =direct force, in lbs

d'' = d - t/2, in inches

d = effective depth, in inches

 f_s = steel stress, in psi

A = equivalent area, in sq. inches per ft of width

 A_{s} = area, in sq. inches per ft of width

As stated in the criteria on page 16, solutions requiring the use of compression steel in bending are not acceptable since this in turn requires the use of stirrups or ties around the compression steel. Compression steel is not required if the actual effective depth at a section is not less than the effective depth required for balanced working stresses. Thus, if

$$d < d_{hal}$$

where

$$d_{\text{bal}} = \left(\frac{12M_{\text{S}}}{\frac{1}{2}f_{\text{c}}k_{\text{jb}}}\right)^{1/2}$$

and

$$k = k_{bal} = 0.3902$$

$$j = j_{bal} = 0.8699$$

the effective depth is insufficient. If this condition has not already occurred more than an arbritrarily selected number of times (currently 9) the thickness of the particular section and slab is incremented so that $d \ge d_{bal}$. New unit loads incorporating corrected dead load effects are established, new indeterminate analyses are obtained, and new designs are attempted.

Unusual case, direct compressive force at small eccentricity. - In a few cases, where the direct force is compression and the moment is relatively small, the normal tension control theory for obtaining required area does not apply. This occurs when

$$(z = \frac{M_S}{N}) < (z_{bal} = 0.8699d)$$

These cases are considered in the compression control range in accordance with ACI 318-63 section 1407(b). Equation (14-9) may be used to derive an equation for an equivalent axial load from which the required steel area may be obtained. The equation for equivalent axial load may be written

$$P = G(1 + CD \frac{e}{t})N$$

See ACI Publication SP-3; from Table 26, for $f_s = 16000$ psi and small p_g values, take CD = 4.0, from Table 23 for $f_c' = 4000$ psi, $f_s = 16000$ psi and small p_g values, take G = 0.64. For design, P is taken as the larger of

$$P = 0.64(1 + 4\frac{e}{t})N$$

or

$$P = N$$

From ACI Code sections 1402 and 1403

$$P = 0.85 Ag(0.25 f_c' + f_s p_g)$$

or the total required steel area is

$$A = \frac{1}{16000} \left(\frac{P}{0.85} - 12000t \right)$$

Assuming the opposite side of the section has at least $p_t = 0.001$, i.e., 0.00lbt = 0.012t sq. in. of steel, the steel area required on the side under consideration is

$$A_s = \frac{1}{16000} (\frac{P}{0.85} - 12000t) - 0.012t$$

or

$$A_{s} = \frac{1}{16000} \left(\frac{P}{0.85} - 12000t \right) - 0.384$$

if t exceeds 32 inches.

In these relations

e = 12M/N = eccentricity of direct compressive force, in inches

P = equivalent axial load, in lbs

 $f_{c}' = 4000 \text{ psi}$

 $A_g = gross$ area of column, in sq. inches $p_g = gross$ steel ratio

Unusual case, direct tensile force at small eccentricity. - It is possible for the direct force in pressure conduits to be tension. the direct force is tension and the bending moment is relatively small, the normal tension control theory does not hold. This occurs when

$$M_S \leq 0$$

These cases are considered in the direct tension range. The total required steel area is

$$A = -\frac{N}{20000}$$

Again, assuming the opposite side of the section has at least $p_t = 0.001$, i.e., 0.001bt = 0.012t sq. inches of steel, the steel area required on the side under consideration is

$$A_{\rm S} = -\frac{N}{20000} - 0.012t$$

or

$$A_{s} = -\frac{N}{20000} - 0.384$$

if t exceeds 32 inches.

Load Combinations Producing Maximum Required Areas

Selection of the load combination or combinations that may produce maximum required steel area at a given location may be accomplished by experience, intuition, analysis, or combinations of these. It can not always be ascertained beforehand whether a particular function exists. However, if the function exists, the load combination or combinations that will produce the function can be determined.

Maximum moment plus associated direct force. - Table 1 lists the basic set or sets of loads and the external load combination for each design mode which may give maximum required steel areas at the midspans of the top slab, sidewall, and bottom slab. These results were determined by considering influence lines of the types shown for $M_{\rm A}$ and $M_{\rm C}$ in Appendix A and by considering deflected shapes due to internal water loads.

Table 1 . Loadings for midspan moments

Location	Earth Fou	ndation	Rock Foundation		
(See Figure 1)	No Internal Water	With Internal Water	No Internal Water	With Internal Water	
1	Bl-LC#1	B2-LC#1 or B3-LC#1	Bl-LC#1	B2-LC#1 or B3-LC#1	
2	Bl-L C# 2	Bl-LC#2 or B3-LC#2	Bl -LC#5	Bl-I <i>c#</i> 5 or B3-I <i>c#</i> 5	
7	Bl-LC#2	Bl-Lc#2 or B3-Lc#2	B1-LC#5	BL-LC#5 or B3-LC#5	
8	Bl-LC#1	B2-LC#1 or B3-LC#1	Bl-IC#1	B2-LC#1 or B3-LC#1	
13	Bl-I <i>C#</i> l	B2-LC#1 or B3-LC#1	Bl-LC#1	B2-LC#1 or B3-LC#1	
14	Bl-LC#2	Bl -Lc#2 or B3-Lc#2	Bl -LC#5	Bl-IC#5 or B3-IC#5	

Table 2 lists the basic set of loads and the external load combinations for each design mode which may give maximum required steel areas at the faces of supports. These results were determined by considering influence lines of the type shown for MB in Appendix A and by considering deflected shapes due to internal water loads. Alternate load combinations are given in some cases. The influence lines for moment correctly indicate the load combination producing maximum moment. However, the alternate load combination, although producing a smaller moment, may require a greater steel area because of the smaller direct force involved.

Table 2. Loadings for moments at face of supports.

	Earth Foundation			Rock Foundation				
Location (See Figure 1)	Infli	rom lence ine	Alternate		From Influence Line		Alternate	
	No Internal Water	With Internal Water	No Internal Water	With Internal Water	No Internal Water	With Internal Water	No Internal Water	With Internal Water
3		B3-LC#0				в3 -LC #О		
14	Bl-LC#3	BL-LC#3	Bl-LC#1	Bl -LC#1	Bl-Lc#6	Bl -LC#6	Bl-LC#4	Bl -LC#4
5		в3 -Lc# 0				B 3 - LC#0		
6	Bl-LC#3	Bl -LC#3	Bl -LC #2	Bl-LC#2	Bl-LC#6	Bl-LC#6	Bl <i>-</i> LC#5	Bl - LC#5
9		B3 -LC #0			Bl-LC#4	B3 -LC #4		
10	Bl-LC#3	Bl-LC#3	Bl-LC#2	Bl - L c #2	Bl-LC#3	Bl -LC #3	Bl-LC#2	Bl-LC#2
11		в3 - Lc#0			Bl-LC#4	B3 -LC #4		
12	BlLC#3	Bl-LC#3	Bl-LC#1	Bl-LC#1	BL-LC#3	Bl-LC#3	Bl-LC#1	Bl-LC#1

The conclusions reached in Table 2 neglect the fact that the maximum moment at a face of a support may be caused by a load combination other than the one producing the maximum corner moment. Thus Table 2 is not sufficient by itself to always determine maximum required steel areas at faces of supports. Table 3 supplements the previous table. It lists additional basic sets of loads and external load combinations which may give maximum areas at faces of supports. These additional results were determined by considering influence lines of the type shown in Appendix A for M at face of support in the top slab.

Table 3. Additional loadings for face moments

Location	Earth Foundation		Rock Foundation		
(See Figure 1)	No Internal Water	With Internal Water	No Internal Water	With Internal Water	
3	Bl-IC#1	B2-IC#1 or B3-IC#1	BL-IC#1	B2 -IC# l or B3 -IC# l	
4	Bl-IC#2	Bl-IC#2	Bl - LC#5	BL-LC#5	
5	Bl-IC#2	Bl-IC#2 or B3-IC#2	Bl -I.C #2	Bl-IC#2 or B3-IC#2	
6	Bl-IC#1	BL-LC#1	Bl -IC# 4	Bl <i>-</i> LC#4	
9	Bl-IC#2	Bl <i>-</i> I <i>C#</i> 2 or B3-I <i>C</i> #2	Bl -LC#6	Bl-LC#6 or B3-LC#6	
10	Bl-LC#1	Bl-IC#1	Bl -IC#1	Bl-IC#1	
11	Bl-IC#1	B2-IC#1 or B3-IC#1	Bl - I <i>C#</i> l	B2-LC#1 or B3-LC#1	
12	Bl-LC#2	Bl-I <i>C#</i> 2	. Bl <i>-</i> LC#5	BL-LC#5	

Maximum direct force plus associated moment. - Occasionally the maximum required steel area is governed by the maximum direct force plus associated moment rather than by maximum moment plus associated direct force. Maximum compressive direct forces occur with the conduit empty. Maximum tensile direct forces in the top slab and sidewalls occur, if they occur, with the conduit flowing full under pressure. The bottom slab, if the conduit is on rock, may carry direct tension when the conduit is empty. Table 4 lists the basic set of loads and external load combinations producing these maximum direct forces.

Member	Compression	Tension	
Top Slab	On earth Bl-IC#2 On rock Bl-IC#6	B3-LC#0	
Sidewalls	Bl-IC#1	B3-LC#0	
Bottom Slab	Bl -I.C#3	On earth B3-IC#O On rock B3-IC#4 On rock B1-IC#4	

Table 4 . Loadings for maximum direct forces

Procedure at a Section

With the corner moments known for all external and internal loads, the design moment and direct force at a given section may be computed by statics for each of the basic sets of loads and external load combinations that must be considered. This is illustrated below for six locations and loadings. With the moment and direct force at a section known, the required steel area of interest can be determined as described beginning on page 31.

Location 4 - negative bending moment with loading Bl-IC#3. - Care must be exercised to ensure that statical moment, bending moment, and Slope Deflection moment signs are not confused and to ensure that units are accounted for correctly. To obtain the negative bending moment at the face of the support of the top slab for the indicated loading, observe Figure 23 and note the Slope Deflection sign of M_{BZ} is positive. Then from statics and symmetry, letting M_{BL} be the desired moment

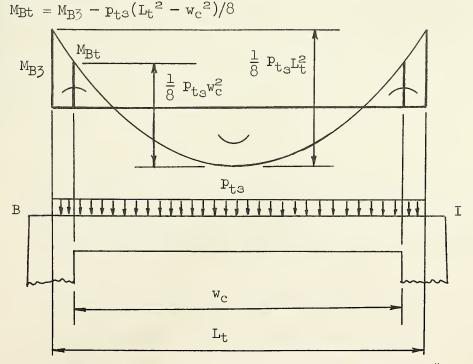


Figure 23. Moments in top slab with loading Bl-LC#3.

If, as written, $M_{\rm Bt} < 0$ the desired moment does not exist. The associated direct force in the top slab may be obtained as the sum of three components, see Figure 24

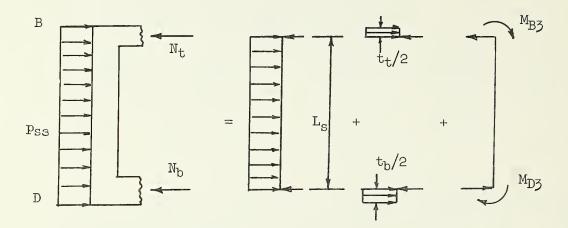


Figure 24. Components of direct force in top and bottom slabs with loading Bl-LC#3.

Thus, noting the component due to corner moments is written for positive Slope Deflection signs

$$N_t = p_{ss}(L_s/2 + t_t/24) + (M_{B3} + M_{D3})/L_s$$

where moments are in ft-lbs and

 $p_{S3} = sidewall$ unit load, in psf

 N_{t} = direct force in top slab, in lbs

Lt = top slab span, in ft

 L_s = sidewall span, in ft

wc = clear width of conduit, in ft

tt = inches

With $M_{\rm Bt}$ and $N_{\rm t}$ known, the required steel at location 4 (negative steel at face of support of top slab) can be determined for the indicated loading.

Location 6 - negative bending moment with loading Bl-LC#3. - Due to the lack of sidewall symmetry, the negative bending moment at the face of the top support of the sidewall for the indicated loading is best obtained by first computing the sidewall reaction at the top and then using the free body diagram shown in Figure 25.

Thus from statics, letting M_{Rs} be the desired moment

$$R = p_{s3}L_s/2 + (M_{B3} + M_{D3})/L_s$$

$$M_{Bs} = M_{B\bar{3}} - Rt_t/24 + p_{s3} t_t^2/1152$$

$$N_{s} = p_{ts}(L_{t} + t_{st}/12)/2$$

If, as written, $M_{\rm BS} < 0$ the desired moment does not exist. With $M_{\rm BS}$ and $M_{\rm S}$ known, the required steel at location 6 (negative steel at face of top support of sidewall) can be determined for the indicated loading.

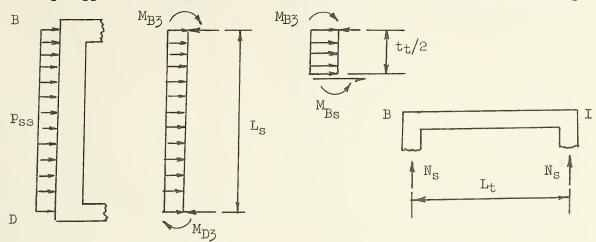


Figure 25. Moment and direct force in sidewall with loading Bl-LC#3.

Location 1 - positive bending moment with loading B2-LC#1. - This case includes internal hydrostatic sidewall loading due to the conduit flowing full as an open channel.

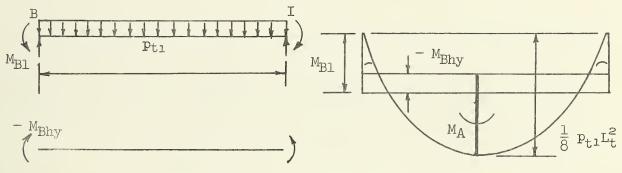


Figure 26. Moments in top slab with loading B2-LC#1.

The moment at B due the hydrostatic loading is $M_{\rm Bhy}$; by Slope Deflection signs, it is a negative moment. Thus from statics, letting $M_{\rm A}$ be the desired moment

$$M_{A} = \frac{1}{8} p_{t1} L_{t}^{2} - M_{Bl} + (-M_{Bhy})$$

If, as written, $M_A < 0$ the desired moment does not exist. The associated direct force may be obtained as the sum of four components, see Figure 27. The direct force in the top slab decreases as the external sidewall load approaches a triangular distribution. Required steel area increases as the direct force decreases. The first component of the direct force is therefore adjusted to partially account for a trapezoidal distribution. Hence

$$N_{t} = P_{sl}(L_{s}/3 + t_{t}/24) - (\frac{1}{2}P_{hy}h_{c})(h_{c}/3 + t_{b}/24)/L_{s} + (M_{Bl} + M_{Dl} + M_{Bhy} + M_{Dhy})/L_{s}$$

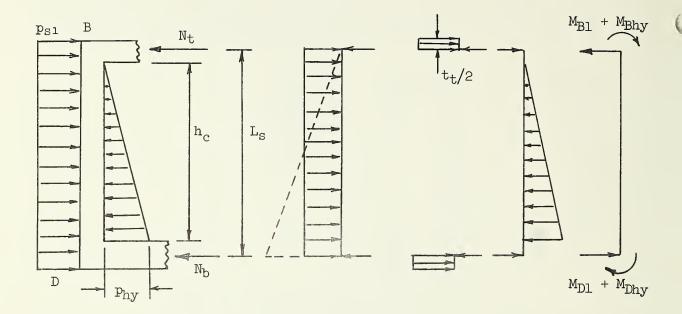


Figure 27. Components of direct force in top and bottom slabs with loading B2-LC#1

With M_A and N_t known, the required steel at location 1 (positive steel in center of top slab) can be determined for the indicated loading.

Location 7 - positive bending moment with loading B3-LC#2. - This case includes internal water loads due to the conduit flowing full as a pressure conduit. It will produce maximum required area for conduits on earth foundations only when the proportions of the conduit are such that the moment at the center of the sidewall due to internal pressure head is positive and larger in magnitude than the moment due to internal hydrostatic sidewall loading. Normally loading B1-LC#2 will govern this location. With either loading, the section of maximum positive moment is unknown due to the lack of symmetry. This section is located and the moment evaluated. The steel required at this section is determined and recorded for location 7.

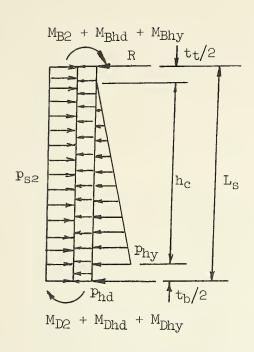
From Figure 28 noting the corner moments are written for positive Slope Deflection signs and thus any negative values are automatically correct

$$R = (p_{s2} - p_{hd})L_{s}/2 - (\frac{1}{2}p_{hy} h_{c})(h_{c}/3 + t_{b}/24)/L_{s}$$

$$+ (M_{B2} + M_{Bhd} + M_{Bhy} + M_{D2} + M_{Dhd} + M_{Dhy})/L_{s}$$

$$V_{p} = R - (p_{s2} - p_{hd}) x_{p} + \frac{1}{2}p_{hy}(x_{p} - t_{t}/24)(x_{p} - t_{t}/24)/h_{c}$$

The section of maximum positive moment is determined by setting $V_p=0$ and solving for x_p . With little error, the last term $(x_p-t_t/24)/h_c$ may be taken as 1/2, then



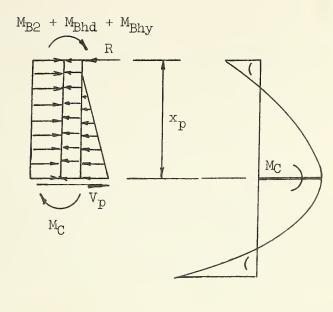


Figure 28. Moments in sidewall with loading B3-LC#2

$$x_{p} = \frac{R - p_{hy} t_{t}/96}{p_{s2} - p_{hd} - p_{hy/4}}$$

Finally, letting $M_{\mbox{\scriptsize C}}$ be the desired moment

$$M_{C} = R x_{p} - (M_{B2} + M_{Bhd} + M_{Bhy}) - (p_{s2} - p_{hd})x_{p}^{2/2}$$

$$+ p_{hy}(x_{p} - t_{t}/24)^{3}/(6h_{c})$$

In these expressions moments are in ft-lbs, pressures are in psf, thicknesses are in inches, and distances including x_p are in feet. If, as written, $M_{\rm C} < 0$ the desired moment does not exist. The associated direct force is

$$N_s = (p_{t2} - p_{hd})(L_t + t_{st}/12)/2$$

With M_C and N_s known, the required steel at location 7 (positive steel nominally in center of sidewall) can be determined for the indicated loading. The thickness at the section of maximum positive moment is

$$t = t_{st} + (t_t/2 + 12x_p)/32$$

Bottom slab, section at midspan - maximum direct compression. - The maximum direct compression on the bottom slab is produced by loading Bl-IC#3 and may be obtained as the sum of three components, see Figure 24 used above. The direct force in the bottom slab increases as the external sidewall load approaches a triangular distribution. The first component of the direct force is therefore adjusted to partially account for a trapezoidal load distribution.

$$N_{b} = p_{s3}(2L_{s}/3 + t_{b}/24) - (M_{B3} + M_{D3})/L_{s}$$

If, as written, $N_b \leq 0$ compressive direct force does not exist in the bottom slab.

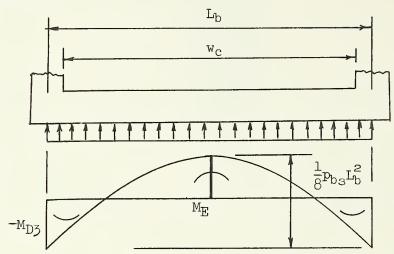


Figure 29. Moments in bottom slab with loading Bl-LC#3.

From statics and symmetry, letting $M_{\rm E}$ be the associated moment and noting by Slope Deflection signs, the corner moment is negative.

$$M_{E} = \frac{1}{8} p_{b3} L_{b}^{2} - (-M_{D5})$$

The sign of M_E is unknown. If M_E is positive as written, the required steel computed from N_b and M_E applies to location 13. If M_E is negative, the required steel applies to location 14.

Bottom slab, section at midspan - maximum direct tension. - The maximum direct tension in the bottom slab is sometimes produced by loading B3-IC#O. Using this loading as an illustration

$$\begin{aligned} \text{M}_{\text{b}} &= (\text{p}_{\text{so}} - \text{p}_{\text{hd}}) \text{L}_{\text{s}} / 2 + \text{p}_{\text{so}} \text{ t}_{\text{b}} / 24 - (\frac{1}{2} \text{ p}_{\text{hy}} \text{h}_{\text{c}}) (2 \text{h}_{\text{c}} / 3 + \text{t}_{\text{t}} / 24) / \text{L}_{\text{s}} \\ &- (\text{M}_{\text{BO}} + \text{M}_{\text{Bhd}} + \text{M}_{\text{Bhy}} + \text{M}_{\text{DO}} + \text{M}_{\text{Dhd}} + \text{M}_{\text{Dhy}}) / \text{L}_{\text{s}} \end{aligned}$$

If, as written, $N_b \ge 0$ tensile direct force does not exist in the bottom slab. From statics and symmetry, letting M_{F} be the associated moment

$$M_{\rm E} = (p_{\rm so} - p_{\rm hd}) L_{\rm b}^2 / 8 - (-M_{\rm DO}) + M_{\rm Dhd} + M_{\rm Dhv}$$

If $\rm M_E$ is positive as written, the required steel computed from $\rm N_b$ and $\rm M_E$ applies to location 13. If $\rm M_E$ is negative, the required area applies to location 14.

Anchorage of Positive Steel

Safe practice requires that the tension in any bar at any section be adequately developed on each side of that section. Thus the inside (positive) steel at the corners of the conduit must be provided sufficient anchorage whenever it is established that tension exists in the bar under some combination of loads. The anchorage may be provided by standard hooks or by embedment length if there is enough distance.

Positive Steel at Face of Support

It is not necessary that separate analyses be performed to establish whether the positive steel at locations 3, 5, 9, and ll is ever in tension. The determinations are made and recorded at the time the required area at these locations is computed. Whenever the tensile area required at one of these locations is greater than zero, then anchorage into the support is required.

Positive Steel at Corner Diagonals

Tension may occur in the inside steel at the corner diagonals even though it is possible tension never occurs in the corresponding steel at the support face. Hence the existence of tension in the inside steel at the diagonals is investigated.

Referring to Figure 30 tension will exist in the bottom steel of sketches (a) through (e) whenever:

for (a), N is tension and M > Nd''/12

for (d), N is zero and M > 0

for (e), N is compression and M > N(t/2 - d/3)/12

recall that compressive direct force is positive and tensile direct force is negative.

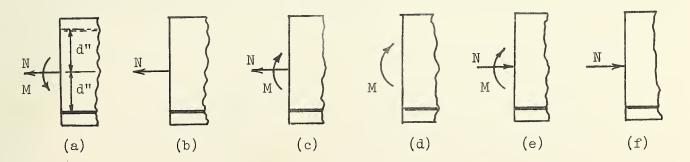


Figure 30. Existence of tension in bottom steel.

The expression M > N(t/2 - d/3)12 comes from $M_{\rm S}$ > N(2d/3)/12 since $M_{\rm S}$ = M + Nd"/12 and d" = d - t/2

Top corner diagonal. - Tension in the inside steel at the top corner can occur only when internal water loading is included in the design. This is loading B3-LC#0. In the analysis of the corner diagonal, the assumption is made that the resultant tensile force in the inside steel, if tension exists, is located approximately at the point on the diagonal where the normal from the point of intersection of the inside steels pierces the diagonal. This point is conservatively taken as 3.535 inches from the inside corner of the conduit.

$$t_k = (t_t^2 + t_{st}^2)^{1/2}$$
 $d_k \approx t_k - 3.535$
 $d_k'' = d_k - t_k/2$

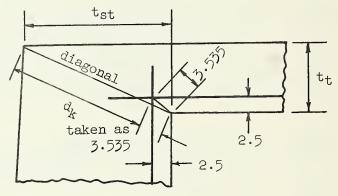


Figure 31. Top corner geometry.

Letting $M_{\rm B}$ be the moment on the corner diagonal and changing signs so that clockwise moments on the diagonal are positive

$$M_{B} = - (M_{BO} + M_{Bhy} + M_{Bhd})$$

the components of the direct force on the diagonal are

$$N_s = (p_{to} - p_{hd})(L_t + t_{st}/12)/2$$

and

$$N_{t} = p_{so}(L_{s}/3 + t_{t}/24) - (\frac{1}{2}p_{hy} h_{c})(h_{c}/3 + t_{b}/24)/L_{s}$$
$$- p_{hd} L_{s}/2 + (M_{BO} + M_{Bhd} + M_{Bhy} + M_{DO} + M_{Dhd} + M_{Dhy})/L_{s}$$

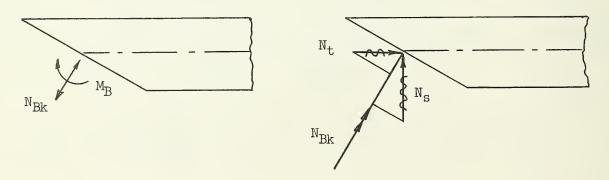


Figure 32. Resultants on top corner diagonal.

The resultant direct force on the diagonal is

$$N_{Bk} = N_t(t_t/t_k) + N_s(t_{st}/t_k)$$

With the resultant moment and direct force on the diagonal known, tests are performed to determine if conditions lie within the limits indicated above, that is, does tension exist on the inside steel at the diagonal.

Bottom corner diagonal. - Tension in the inside steel at the bottom corner can occur with the loadings given in Table 5.

Table 5. Loadings for tension in bottom corner inside steel

Earth Fo	undation	Rock Foundation		
No Internal Water	With Internal Water	No Internal Water	With Internal Water	
	B3 -LC #0	Bl - LC#4	B3 -LC #4	

The analysis for the bottom corner diagonal is similar to that for the top corner. For example, for loading B3-LC#4, letting $\text{M}_{\overline{D}}$ be the moment on the corner diagonal

$$M_D = (M_{D4} + M_{Dhv} + M_{Dhd})$$

and

$$N_s = - p_{hd} (L_b + t_{sb}/12)/2$$

$$\begin{split} \mathbf{N}_{b} &= \mathbf{p_{s4}} (\mathbf{L_{s}}/2 + \mathbf{t_{b}}/24) - (\frac{1}{2}\mathbf{p_{hy}} \ \mathbf{h_{c}})(2\mathbf{h_{c}}/3 + \mathbf{t_{t}}/24)/\mathbf{L_{s}} \\ &- \mathbf{p_{hd}} \ \mathbf{L_{s}}/2 - (\mathbf{M_{B^{h}}} + \mathbf{M_{Bhy}} + \mathbf{M_{Bhd}} + \mathbf{M_{D^{h}}} + \mathbf{M_{Dhy}} + \mathbf{M_{Dhd}})/\mathbf{L_{s}} \end{split}$$

so

$$N_{Dk} = N_b(t_b/t_k) + N_s(t_{sb}/t_k)$$

where

$$t_k = (t_b^2 + t_{sb}^2)^{1/2}$$

With M_{D} and N_{DK} known, tests again discern whether the inside steel at the diagonal is in tension.



Spacing Required by Flexural Bond

Flexural bond stresses must be held within tolerable values whenever a bar is in tension. It is therefore necessary to determine the maximum shear that can exist at any section under consideration when the steel under investigation at the section is acting in tension. This maximum shear is sometimes less than the maximum shear that can ever exist at the section.

Relation to Determine Required Spacing

For steel bar sizes #5 through #11 and for $f_c' = 4000$ psi, the allowable flexural bond stress is inversely proportional to bar diameter, D. Thus the number of bars required per foot of width at a section is independent of bar size. The number of bars required is obtained by

$$n\pi D = \Sigma o = \frac{V}{ujd} = \frac{V}{\left(\frac{C\sqrt{f_C'}}{D}\right)\left(\frac{7}{8}d\right)}$$

or

$$n = \frac{V}{(\pi C \sqrt{f_c^{\dagger}})(\frac{7}{8}d)}$$

Since the number of bars per foot can be determined, the allowable spacing of the bars is obtained by

$$s = \frac{12}{n} = \frac{12\pi C\sqrt{f_c'(\frac{7}{8}d)}}{V}$$

for tension top bars C = 3.4 and

$$s = 7,093d/V$$

for other tension bars C = 4.8 and

$$s = 10,015d/V$$

where

s = center to center spacing of bars, in inches

d = effective depth at the section, in inches

V = shear at the section, in 1bs.

Note that it is theoretically possible to determine the minimum acceptable bar size at a section when required steel area and spacing is given. This is not done since it is felt desirable to allow the exercise of judgement in the selection of actual sizes and spacings of bars.

Load Combinations Producing Minimum Required Spacing

The flexural bond allowable steel spacing at a particular location is computed only after it has been determined the tensile area required in bending at that location is greater than zero. Table 6 lists the basic set

or sets of loads and the external load combinations that may produce maximum shear at the section under consideration when the indicated steel is acting. In some places more than one loading is listed for a particular steel location and design mode. If in a design, it is determined that the steel is in tension at that location then the only loadings investigated to determine the smallest allowable spacing are the loadings which produce tension in the steel for that design.

Procedure at a Section

The computation of bond spacing is illustrated below for three locations in the top slab. Computations for locations in the sidewalls and bottom slab are similar except that conditions in the sidewalls are complicated by the lack of symmetry. Note that the spacings computed for the positive steel at locations 1, 7, and 13 are really the spacings required at the respective points of inflection as shown on Figure 1.

Location 1 - with loading Bl-LC#1. - If tension occurs in the top slab positive steel for this loading: the points of inflection are located, the shear at the points of inflection is obtained, and the required bond spacing is computed.

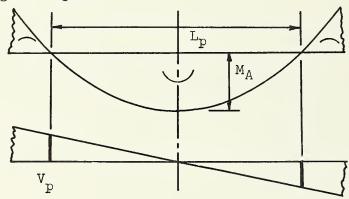


Figure 33. Points of inflection in top slab with loading Bl-LC#1.

From symmetry, assuming ${\rm M}_{\rm A}$ is the moment at the center of the top slab

$$L_{p} = \left(\frac{8M_{A}}{p_{t1}}\right)^{1/2}$$

and

$$V_p = p_{t_1} L_p/2$$

so

$$s = 10,015 \, d_t/V_p$$

where d_t is the effective depth of the top slab.

Location 1 - with loadings B2-IC#1 and B3-IC#1. - When internal water load is included in the design, it is not known beforehand which of the indicated loadings will govern the spacing. Usually the moment at the center of the top slab due to the pressure head loading is negative, when this is so, loading B2-IC#1 controls. However, in some designs

Table 6. Loadings for flexural bond

Location	Earth Foundation		Rock Foundation		
(see Figure 1)	No Internal Water	With Internal Water	No Internal Water	With Internal Water	
1	Bl-LC#1	B2-IC#1 B3-IC#1	Bl-IC#1	B2-LC#1 B3-LC#1	
2	pit en				
3	B1-IC#1	B2-IC#1 B3-IC#1 B3-IC#0	B1 - LC#1	B2-LC#1 B3-LC#1 B3-LC#0	
4	Bl -IC#1 Bl -IC#2	Bl-IC#1 Bl-IC#2	Bl -IC#1 Bl -IC#2	Bl -IC#1 Bl -IC#2	
5	Bl-LC#2	Bl-IC#2 B3-IC#2 B3-IC#0	B1-I <i>C</i> #2	Bl -IC#2 B3-IC#2 B3-IC#0	
6	Bl-LC#0 Bl-LC#2	Bl-IC#0 Bl-IC#2	Bl -I <i>C#</i> 4 Bl -I <i>C#</i> 6	Bl-IC#4 Bl-IC#6	
7	Bl-IC#2	Bl-IC#2 B3-IC#2	Bl-IC#5	BL-LC#5 B3-LC#5	
8		B2-LC#0	Bl -I <i>C#</i> 4	Bl -LC#4 B2-LC#0	
9	B1 - IC#2	Bl -IC#2 B3-IC#2 B3-IC#0	B1 -IC#4 B1 -IC#6	Bl -IC#4 Bl -IC#6 B3-IC#4 B3-IC#6	
10	Bl -IC# l Bl -IC# 3	Bl -LC#1 Bl -LC#3	B1 - I.C#1 B1 - I.C#3	Bl -LC#1 Bl -LC#3	
11	Bl-LC#1	B2-IC#1 B3-IC#1 B3-IC#0	BL-LC#L	B2-IC#1 B3-IC#1 B3-IC#4	
12	Bl -IC#1 Bl -IC#2	Bl -LC#1 Bl -LC#2	Bl-IC#1 Bl-IC#2	Bl-LC#1 Bl-LC#2	
13	Bl-LC#1	B2-IC#1 B3-IC#1	Bl-LC#1	B2-LC#1 B3-LC#1	
14					

this moment may be positive. For illustration assume it is positive, then let M_A " be the moment at the center of the top slab due to loading B2-IC#1 and M_A " be the moment due to loading B3-IC#1. From Figure 34

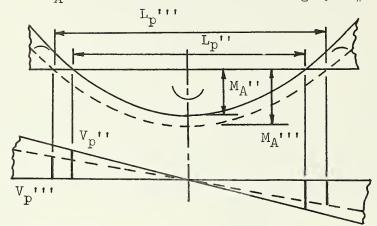


Figure 34. Points of inflection with loadings B2-IC#1 and B3-IC#1.

either $V_p^{\ \ \ }$ or $V_p^{\ \ \ }$ may control spacing. Thus

$$L_{p}" = \left(\frac{8M_{A}"}{p_{t1}}\right)^{1/2}$$
 $L_{p}"' = \left(\frac{8M_{A}"'}{p_{t1} - p_{hd}}\right)^{1/2}$

and

$$V_{p}'' = p_{t1} I_{p}''/2$$
 $V_{p}''' = (p_{t1} - p_{hd}) I_{p}'''/2$

so s'' = 10,015
$$d_t/V_p$$
'' s''' = 10,015 d_t/V_p '''

The smaller spacing with its distance from the center of the span to the point of inflection are taken as the answer.

Location 3 - with loading B3-IC#0. - In some designs loadings B2-IC#1 and/or B3-IC#1 will cause tension in the steel at location 3, if this occurs, they will require a smaller spacing than loading B3-IC#0.

The shear at the face of the support in the top slab for loading B3-LC#O is

$$V_{Bt} = (p_{to} - p_{hd}) w_c / 2$$

so
s = 10,015 d_t / V_{P+}

Location 4 - with loadings Bl-IC#l and Bl-IC#2. - If both loadings cause tension in the steel at location 4, loading Bl-IC#l controls. However, in some designs only loading Bl-IC#2 causes tension in this steel. In either event, the depth below the negative steel is checked to determine whether the steel qualifies as tension top bars or as other tension bars.

Summary of Design

Figure 35 presents a summary flow chart showing the sequence of the design process discussed on the preceding pages. The basic logic of the computer program prepared and used to design the Standard Single Cell Rectangular Conduits parallels this summary flow chart.

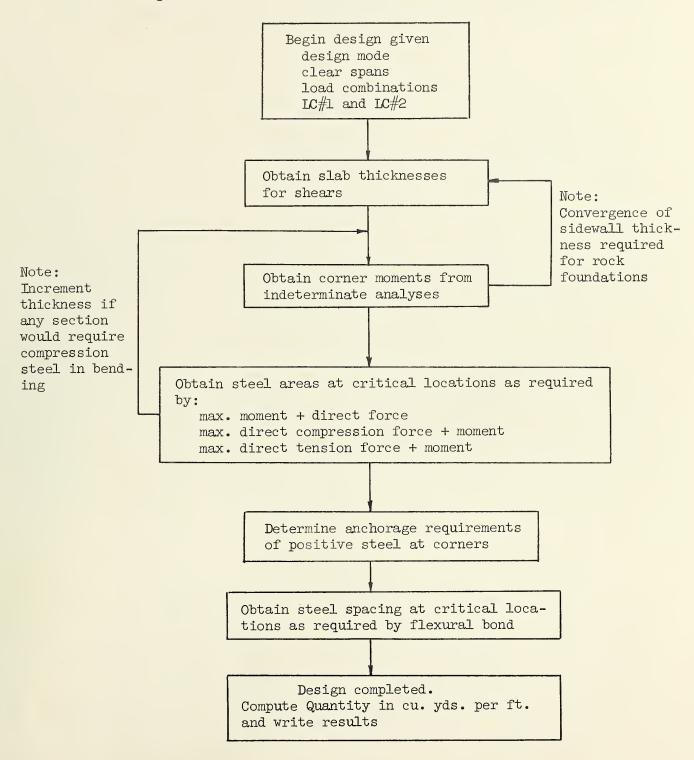


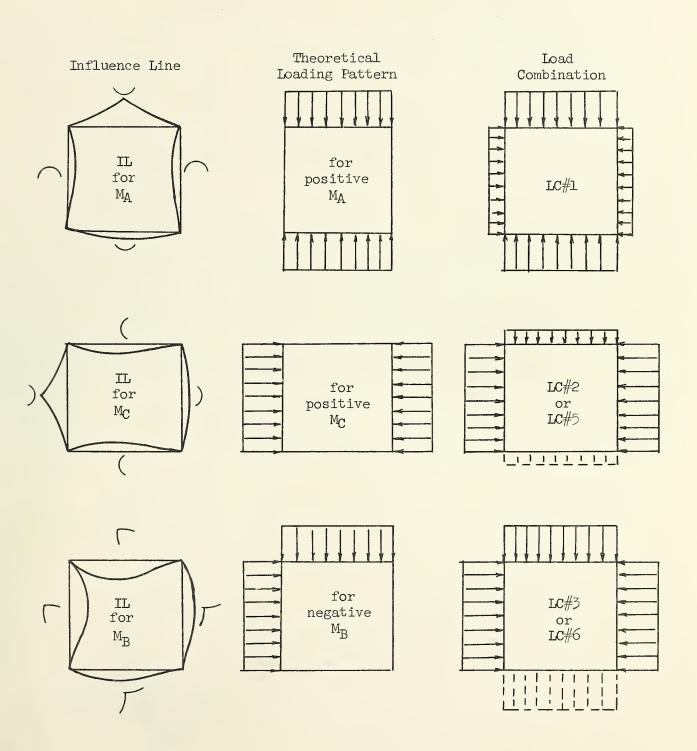
Figure 35. Summary flow chart of design process.



Appendix A

Some Qualitative Influence Lines for Inward Acting Applied Loads

The three influence lines for moment, drawn below, suggest various theoretical loading patterns and actual load combinations as shown.



Three additional influence lines for different functions are given below. These, together with the preceding influence lines, may be used as models to obtain other influence lines as may be desired.

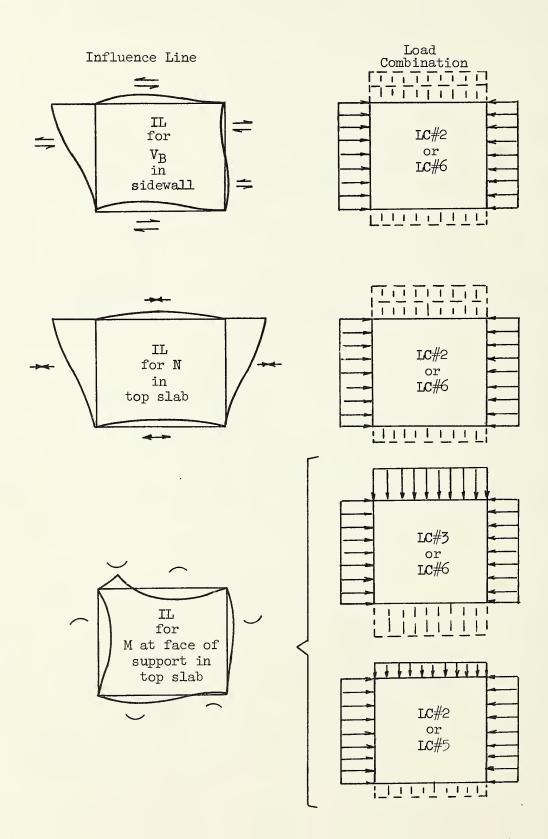
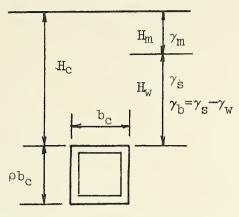


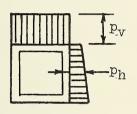
Illustration of Existance of Load Combinations



The following shows one situation which gives rise to various load combinations. Two conditions are recognized.

- (1) Initial (construction) condition Shears along sides of interior prism have not yet developed.
- (2) Developed (long term) condition Shears have completely developed along sides of interior prism.

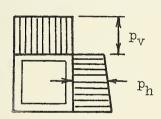
Initial Condition - moist



$$p_{v} = \gamma_{m}H_{c}$$

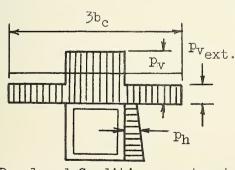
$$p_{h} = K_{o}(\gamma_{m}H_{c} + \gamma_{m}\rho b_{c}/2)$$

Initial Condition - saturated



$$\begin{aligned} \mathbf{p}_{\mathbf{V}} &= \gamma_{\mathbf{m}} \mathbf{H}_{\mathbf{m}} + \gamma_{\mathbf{b}} \mathbf{H}_{\mathbf{W}} + \gamma_{\mathbf{W}} \mathbf{H}_{\mathbf{W}} \\ \mathbf{p}_{\mathbf{h}} &= \mathbf{K}_{\mathbf{O}} (\gamma_{\mathbf{m}} \mathbf{H}_{\mathbf{m}} + \gamma_{\mathbf{b}} \mathbf{H}_{\mathbf{W}} + \gamma_{\mathbf{b}} \rho \mathbf{b}_{\mathbf{c}} / 2) + \gamma_{\mathbf{W}} (\mathbf{H}_{\mathbf{W}} + \rho \mathbf{b}_{\mathbf{c}} / 2) \\ &\text{(Select high } \mathbf{K}_{\mathbf{O}}) \end{aligned}$$

Developed Condition - moist



$$p_{v} = C_{p}\gamma_{m}b_{c} - \text{from TR-5}$$

$$p_{v} = C_{p}\gamma_{m}b_{c} - \text{from TR-5}$$

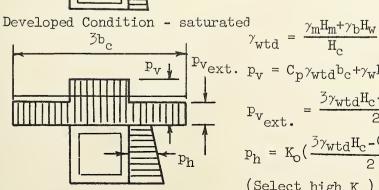
$$p_{v} = \frac{3\gamma_{m}H_{c} - C_{p}\gamma_{m}b_{c}}{2}$$

$$p_{h} = K_{o}(\frac{3\gamma_{m}H_{c} - C_{p}\gamma_{m}b_{c}}{2} + \gamma_{m}\rho b_{c}/2)$$

$$p_{h} = K_{o} \left(\frac{3\gamma_{m}H_{c} - C_{p}\gamma_{m}b_{c}}{2} + \gamma_{m}\rho b_{c}/2 \right)$$

(Select low K_o)

(3bc is an approximation used for design purposes)



$$p_{vext.} p_{v} = C_{p} \gamma_{wtd} b_{c} + \gamma_{w} H_{w}$$

$$p_{vext.} = \frac{3 \gamma_{wtd} H_{c} - C_{p} \gamma_{wtd} b_{c}}{2} + \gamma_{w} H_{w}$$

$$p_{h} = K_{o}(\frac{3\gamma_{wtd}H_{c} - C_{p}\gamma_{wtd}b_{c}}{2} + \gamma_{b}\rho b_{c}/2) + \gamma_{w}(H_{w} + \rho b_{c}/2)$$
(Select high K_{o})

